

# Measuring the Mass and Spin of Dark Matter at a Lepton Collider

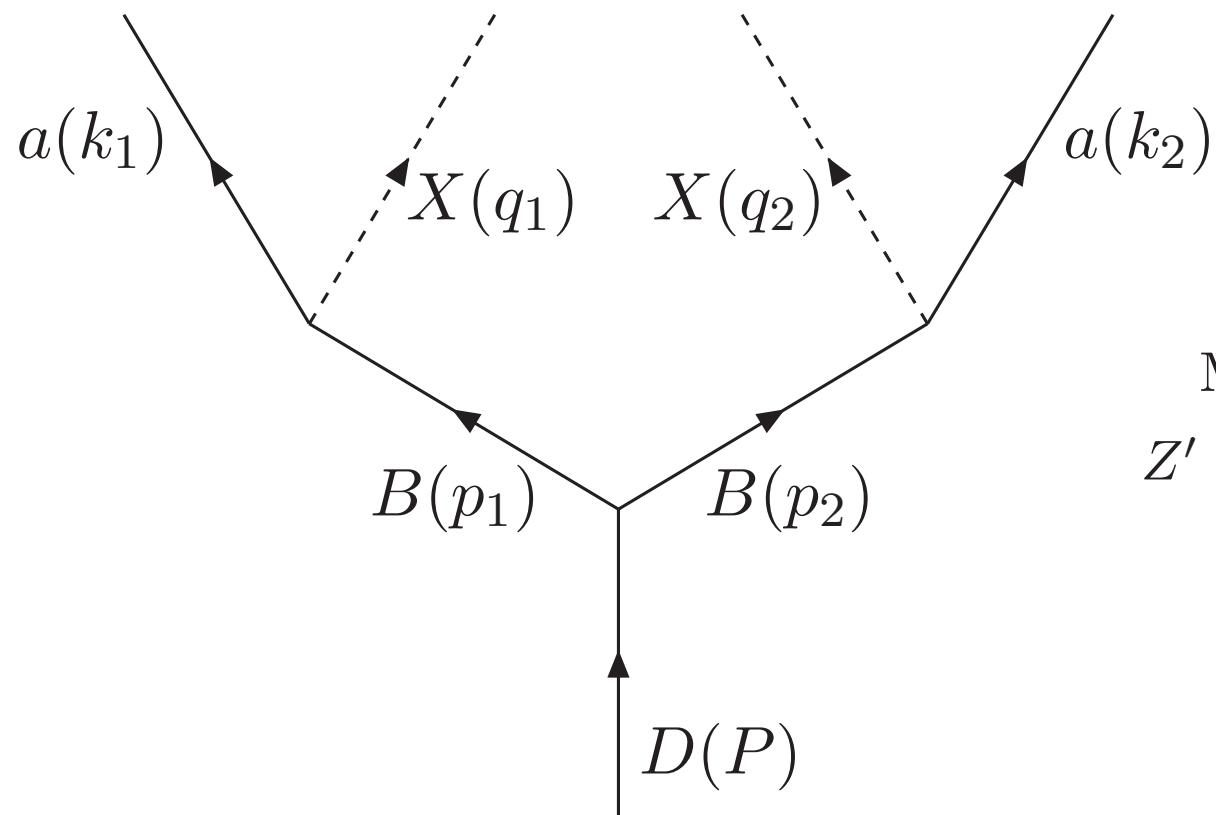
Neil Christensen

PITTSburgh Particle, Astroparticle and Cosmology Center (PITT PACC)

# Dark Matter

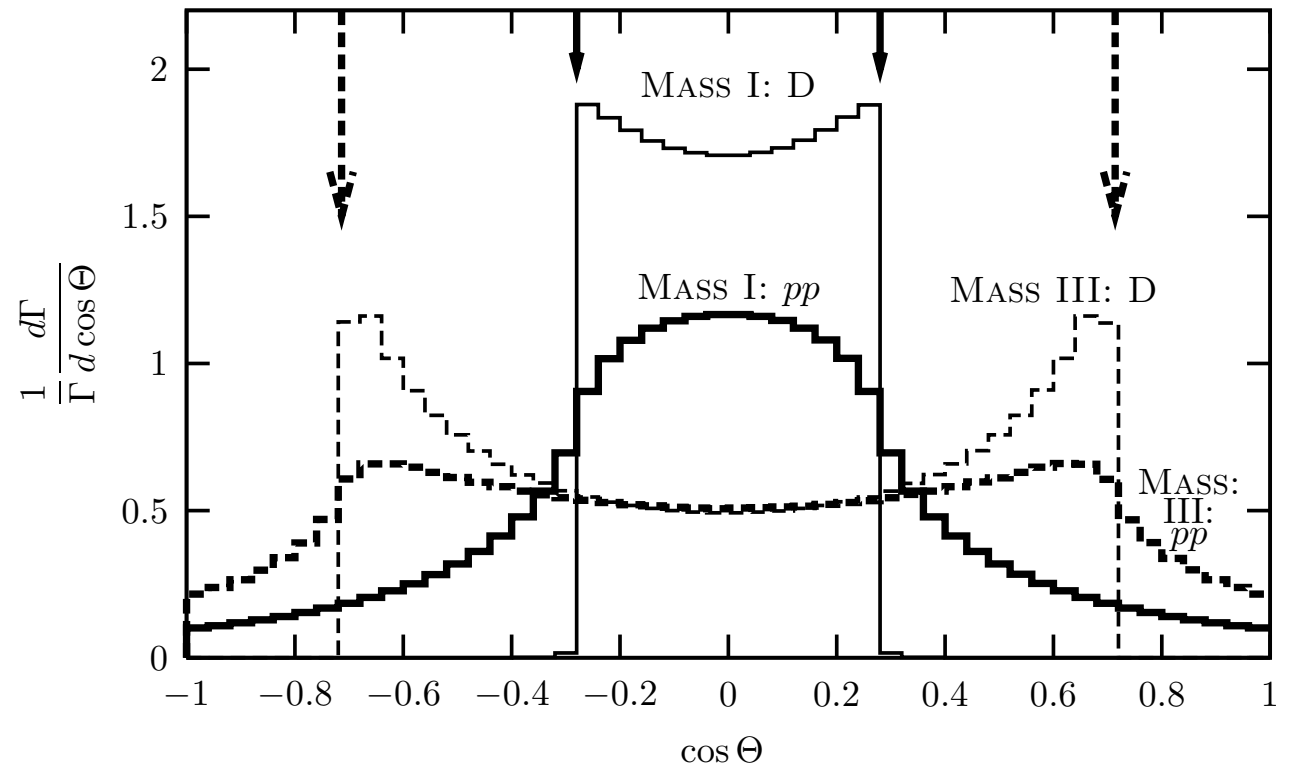
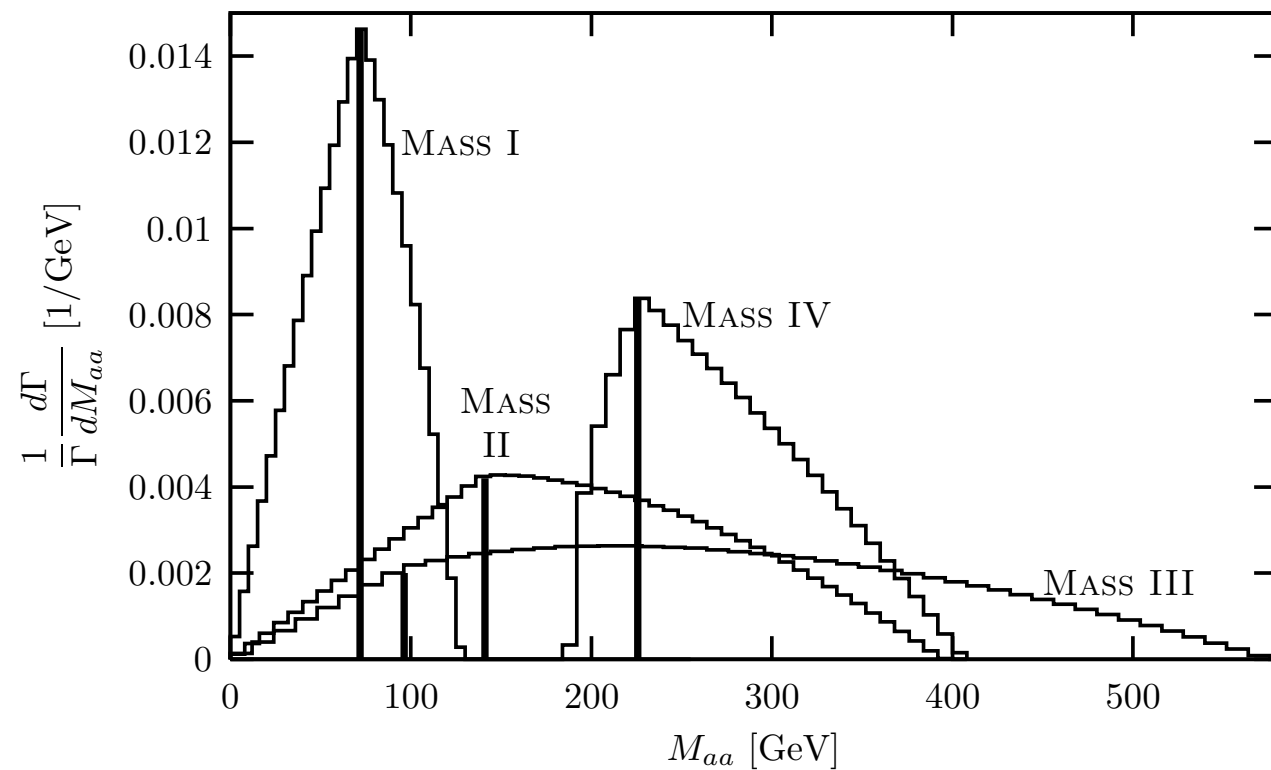
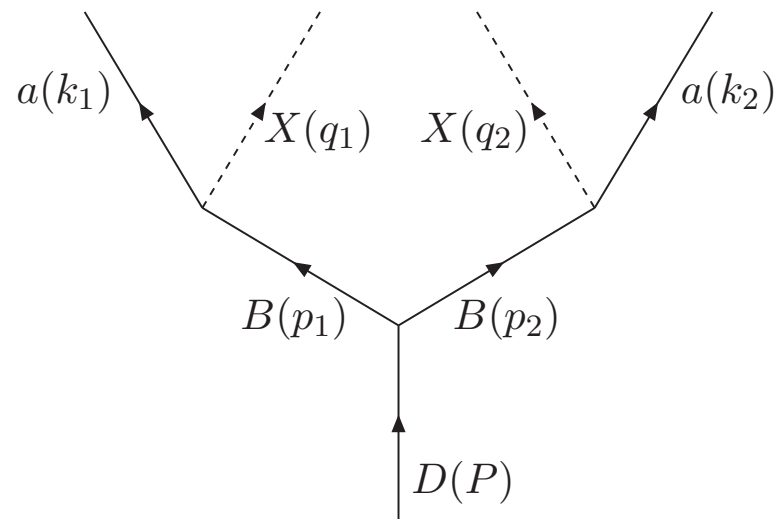
- Existence of dark matter has been well established from astronomical observations.
- Dark matter is non-hadronic and electrically neutral making it difficult to measure its properties.
- Many possibilities for dark matter. WIMPs are well motivated.
- If sufficiently light, WIMPs could be produced at colliders.

# Antlers

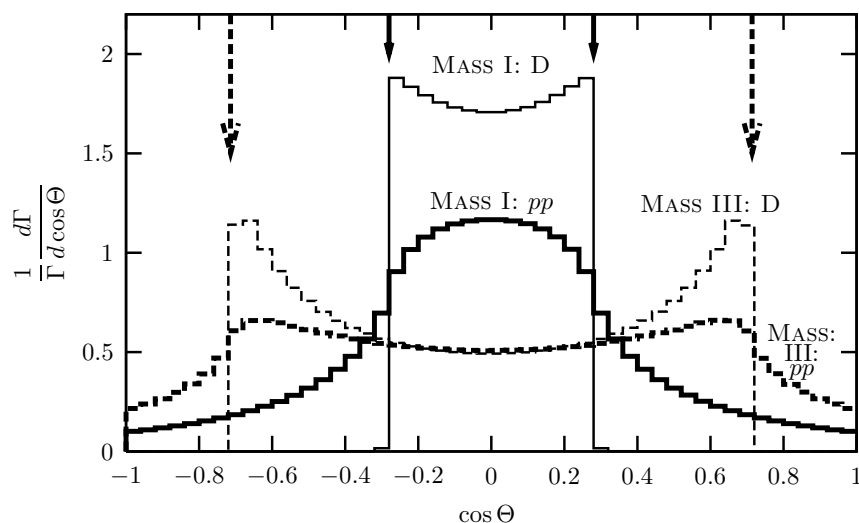
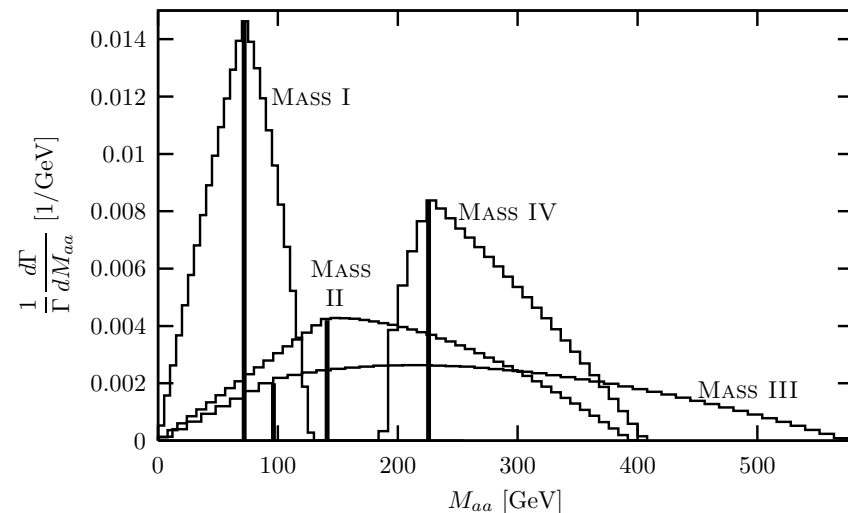
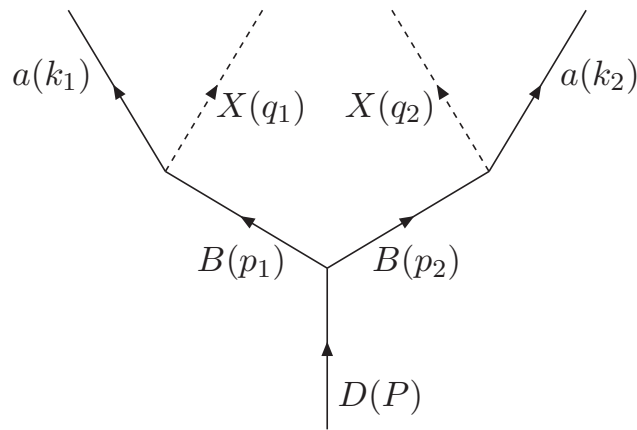


MSSM [7],  $H \rightarrow \tilde{\chi}_2^0 + \tilde{\chi}_2^0 \rightarrow Z\tilde{\chi}_1^0 + Z\tilde{\chi}_1^0$ ;  
 $Z'$  SUSY [8],  $Z' \rightarrow \tilde{\ell}^- + \tilde{\ell}^+ \rightarrow \ell^- \tilde{\chi}_1^0 + \ell^+ \tilde{\chi}_1^0$ ;  
 UED [9],  $Z^{(2)} \rightarrow L^{(1)} + L^{(1)} \rightarrow \ell^- \gamma^{(1)} + \ell^+ \gamma^{(1)}$ ;  
 LHT [10],  $H \rightarrow t_- + t_- \rightarrow tA_H + tA_H$ .

# Kinematic Cusps & Endpoints

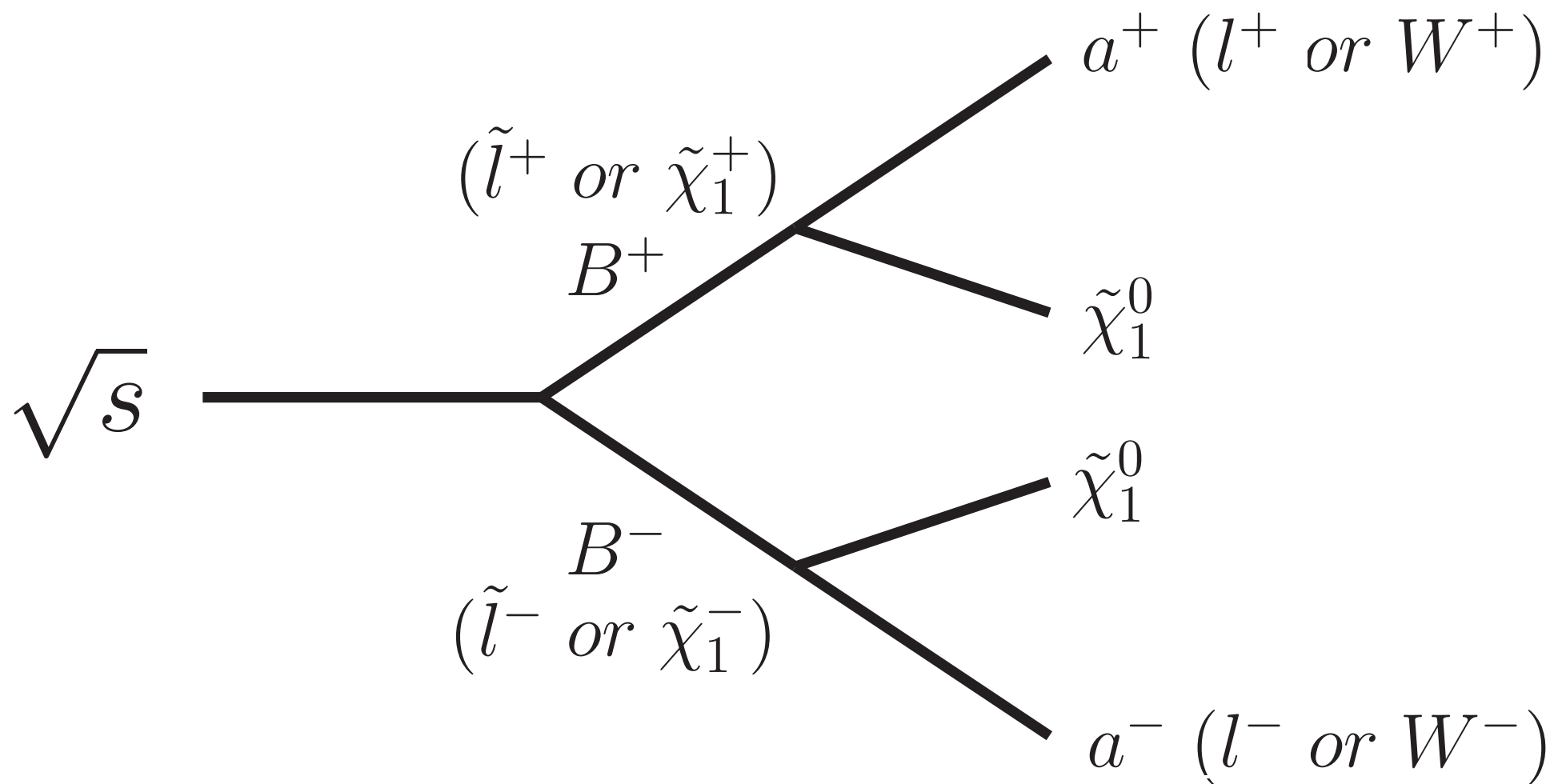


# Kinematic Cusps & Endpoints Challenges

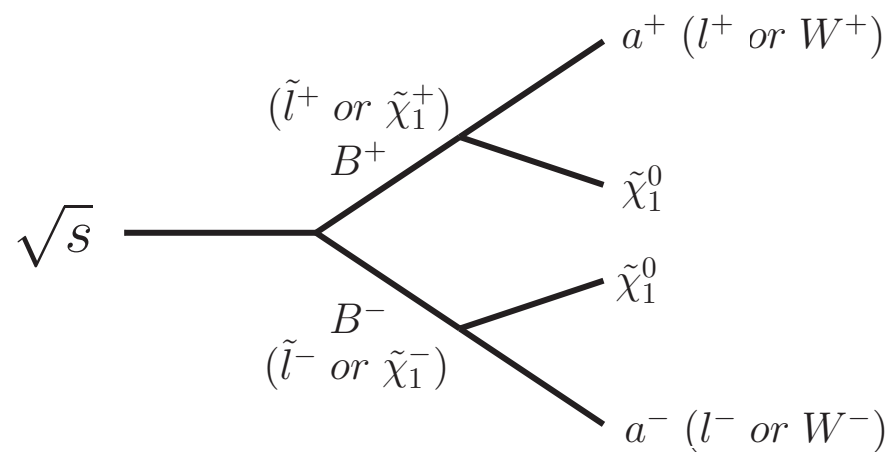


- $D \rightarrow B \rightarrow a$  may not be possible.
- Ex:  $h$  may be too light for  $h \rightarrow 2\tilde{l} \rightarrow 2\tilde{\chi}_1^0 + 2a$
- Cusps or endpoints could be difficult to measure.
- Ex.  $M_{aa} \sim M_Z$
- Ex.  $M_{aa} \sim 0 \text{ GeV}$
- $\cos \theta$  smeared by boost of collision frame.

# Antlers at Lepton Colliders

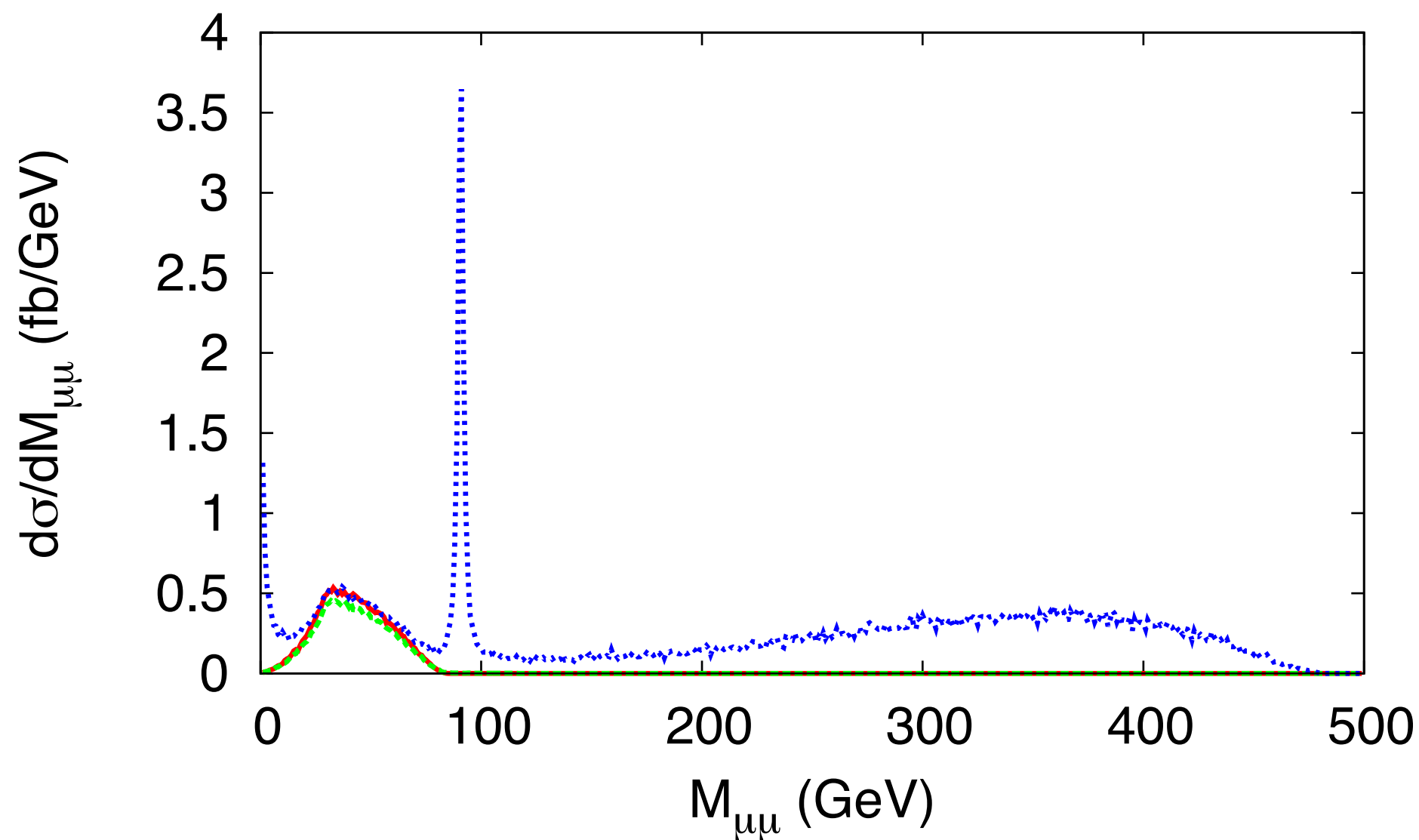


Following slides preliminary: To be published soon:  
Christensen, Han, Song, Stefanus

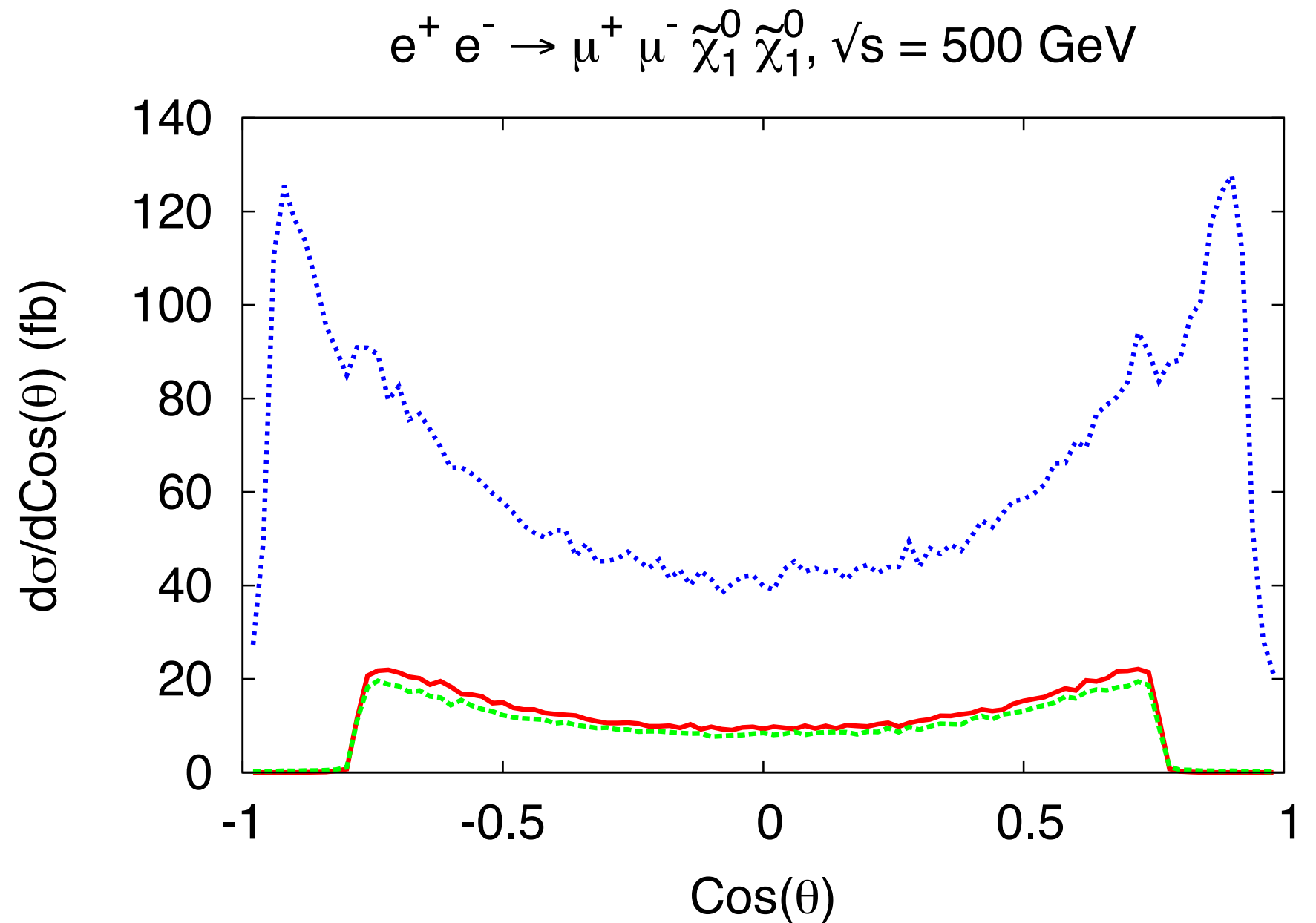
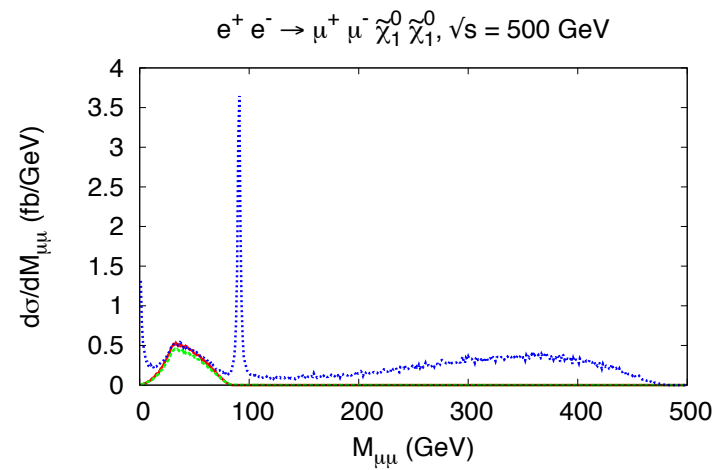
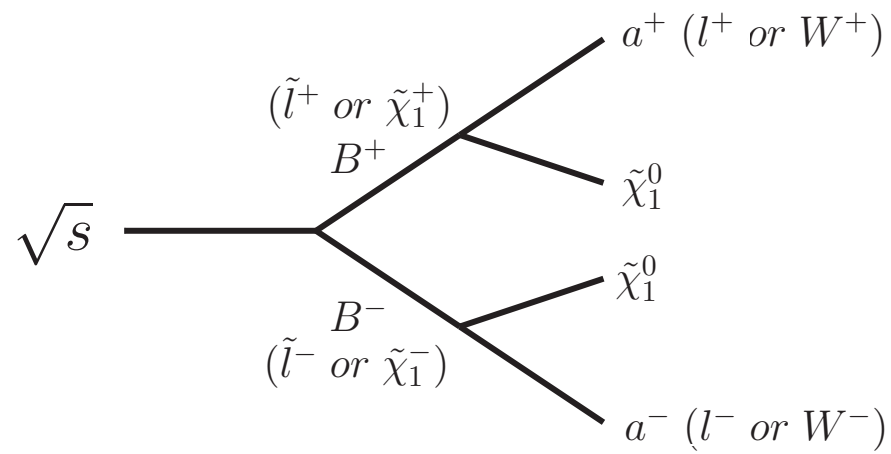


# Antlers at Lepton Colliders

$$e^+ e^- \rightarrow \mu^+ \mu^- \tilde{\chi}_1^0 \tilde{\chi}_1^0, \sqrt{s} = 500 \text{ GeV}$$

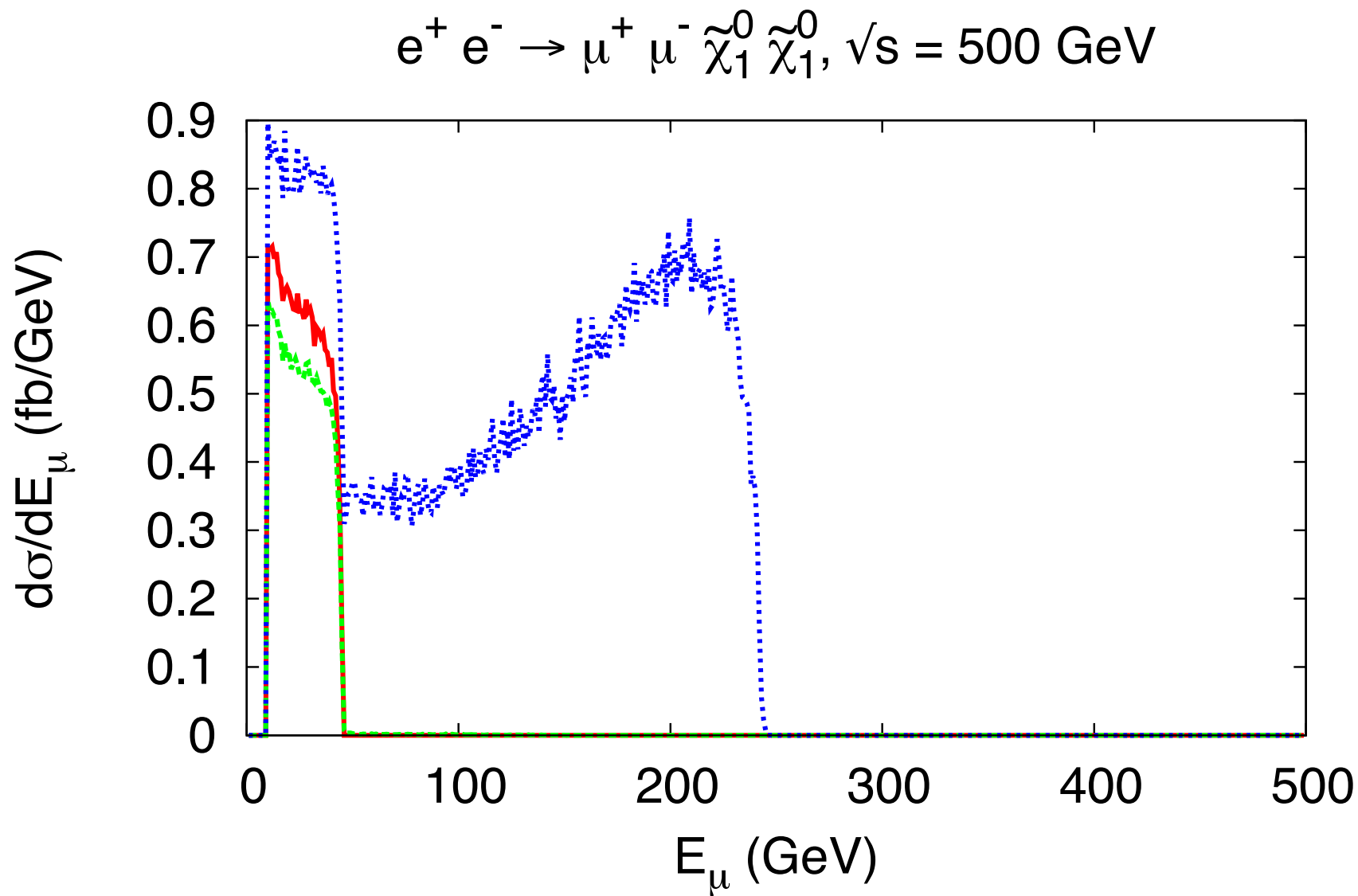
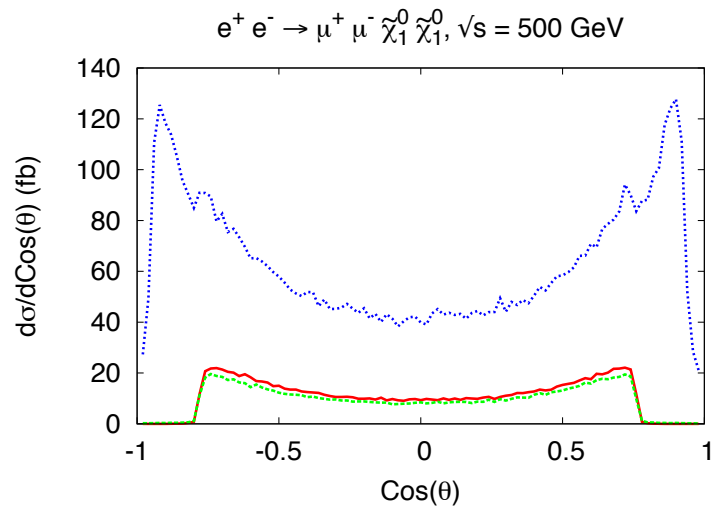
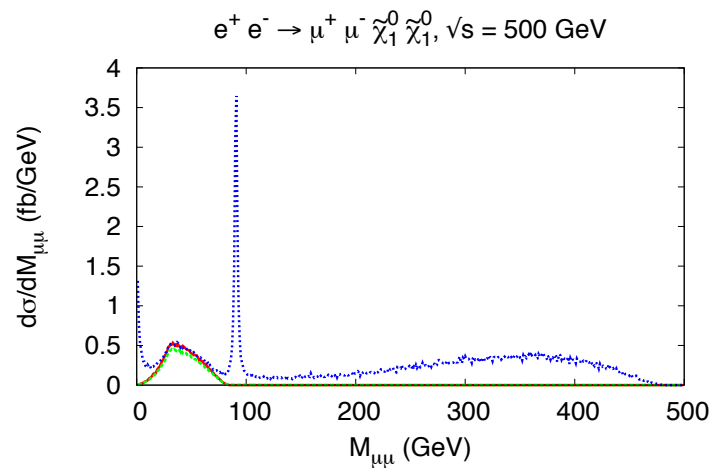
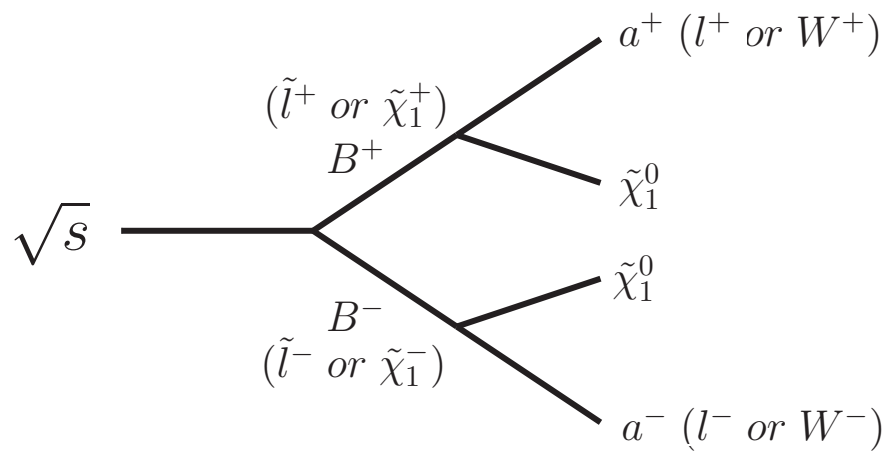


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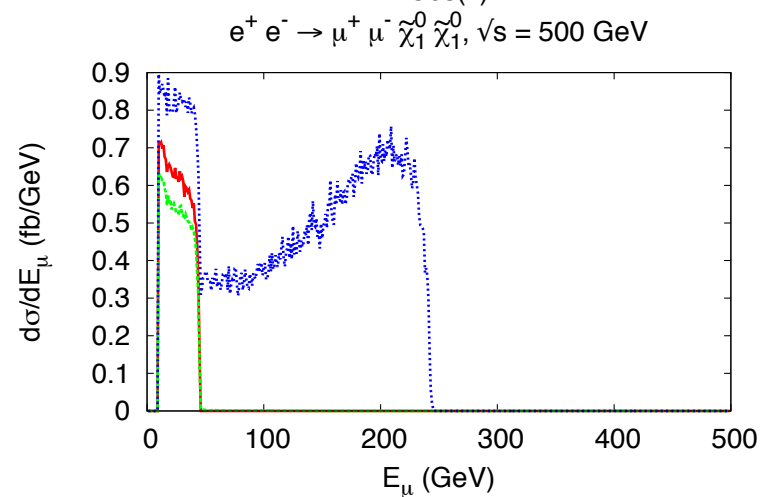
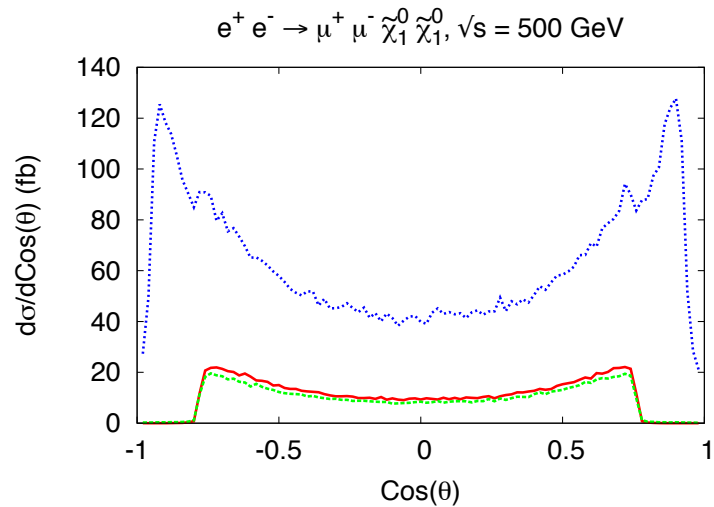
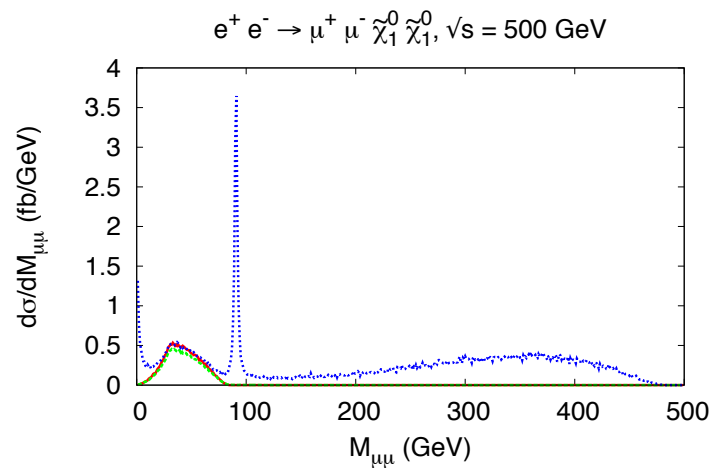
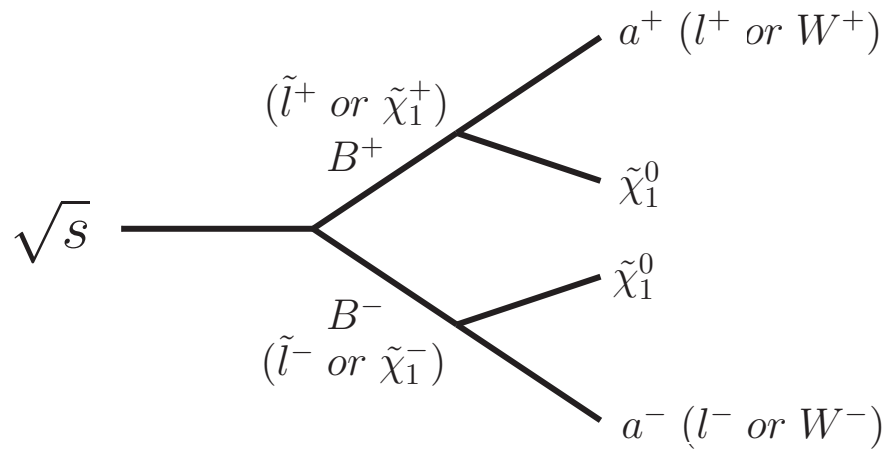




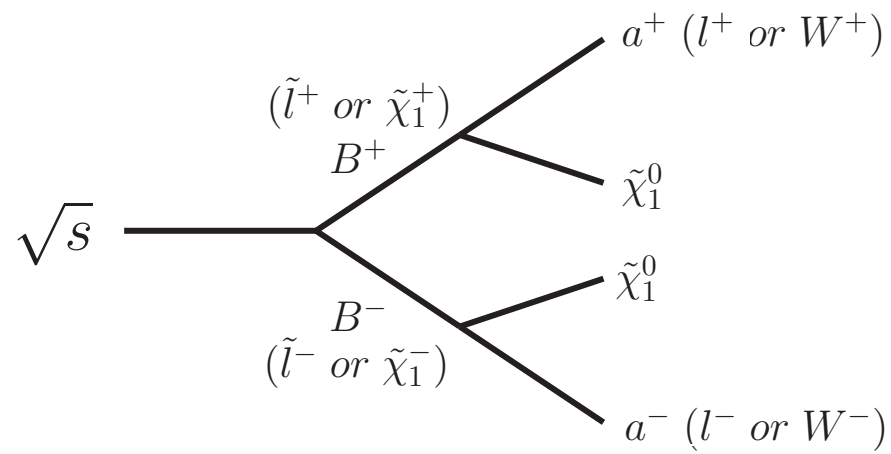
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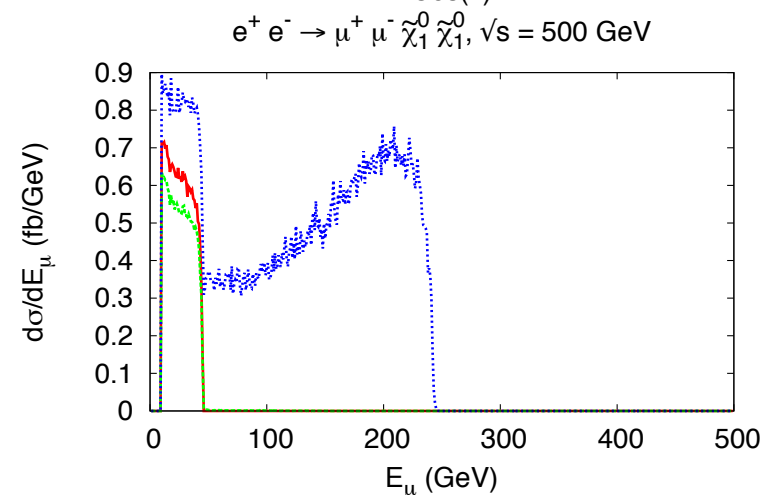
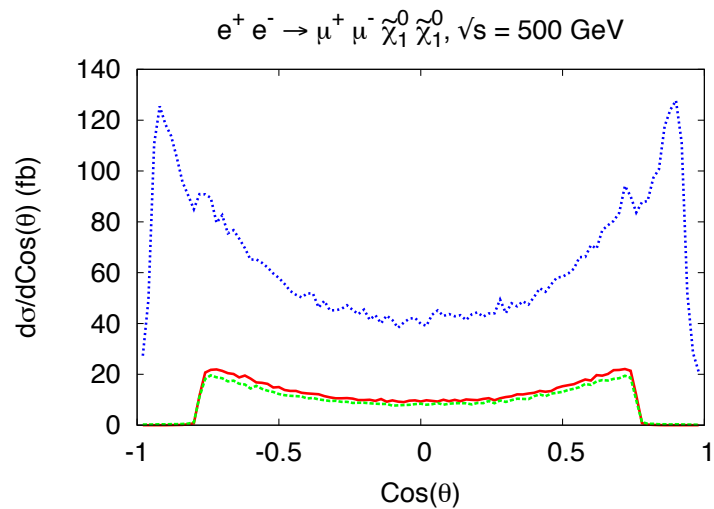
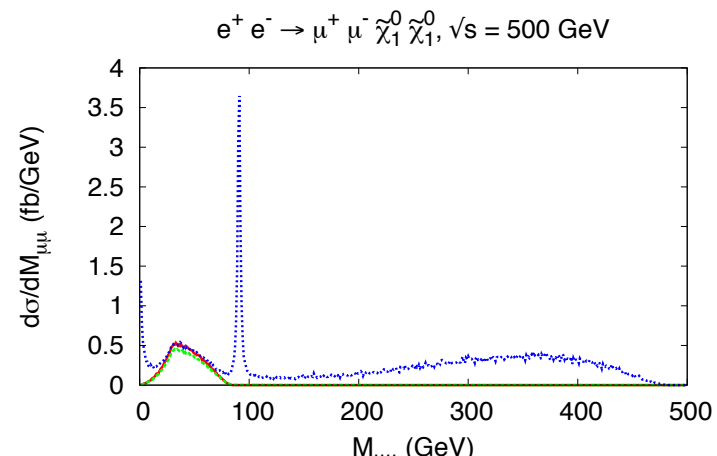
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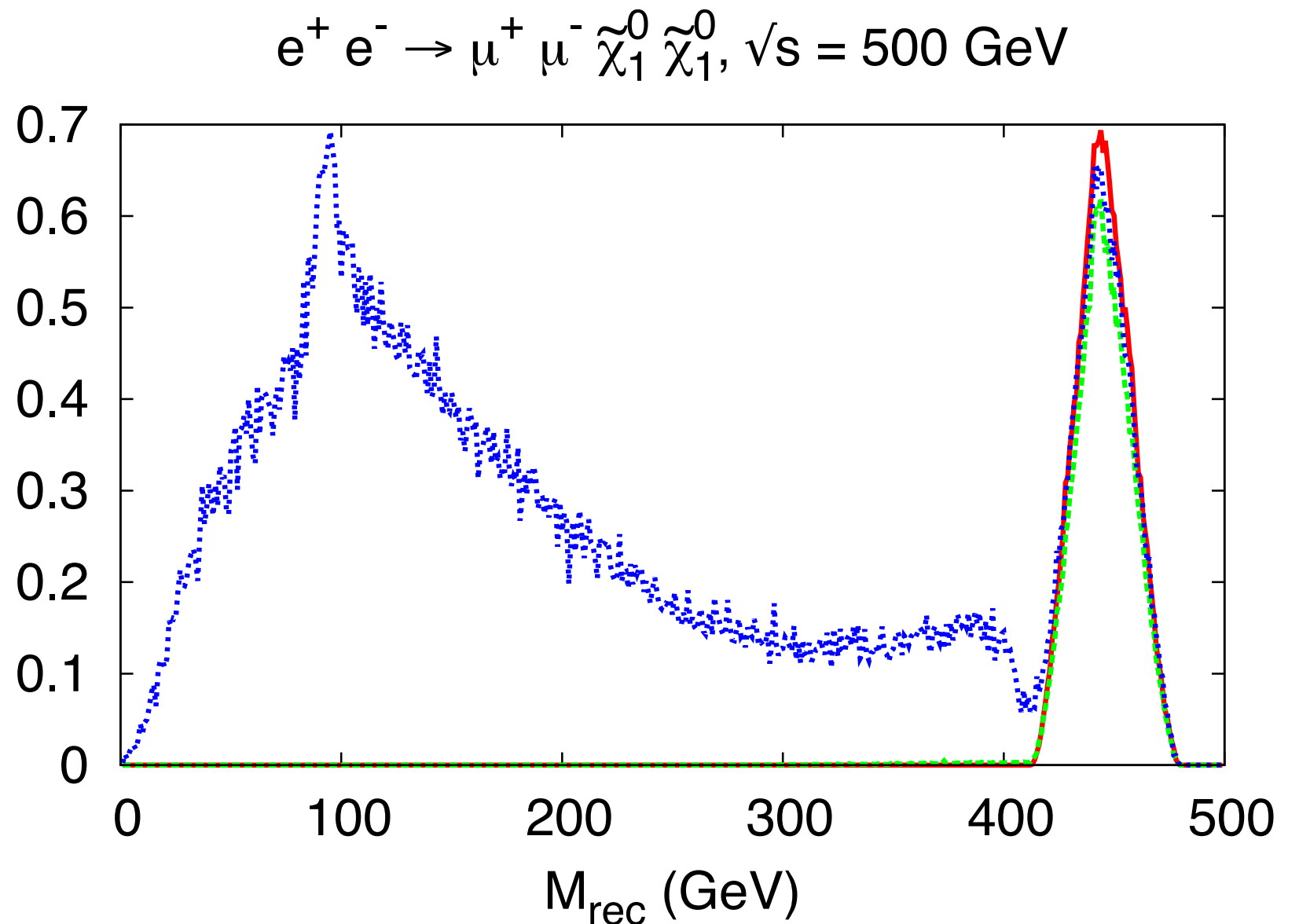
$$m_{rec}^2 \equiv m_{\tilde{\chi}_1^0 \tilde{\chi}_1^0}^2 = s - 2\sqrt{s} (E_{a_1} + E_{a_2}) + m_{aa}^2$$



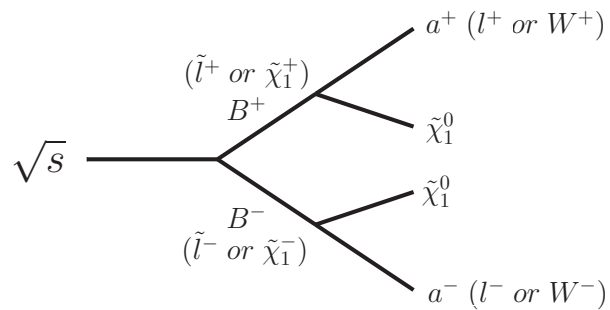
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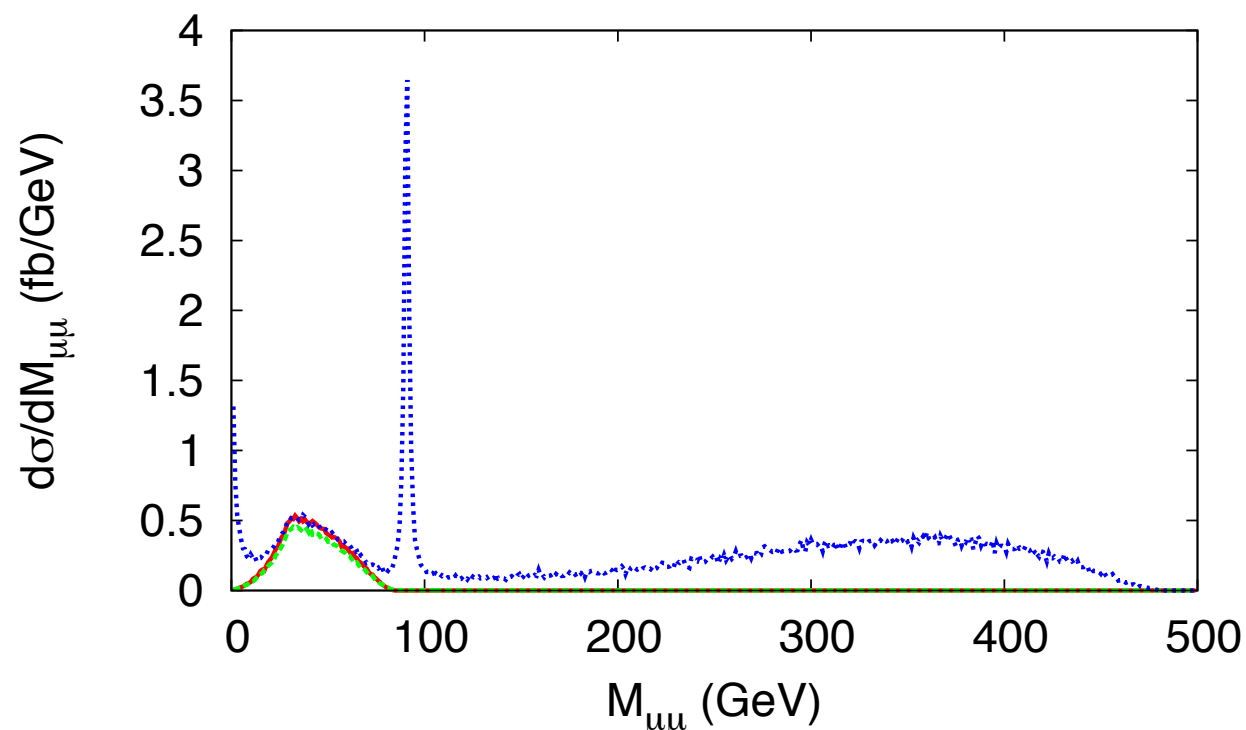
$d\sigma/dM_{\text{rec}} \text{ (fb/GeV)}$



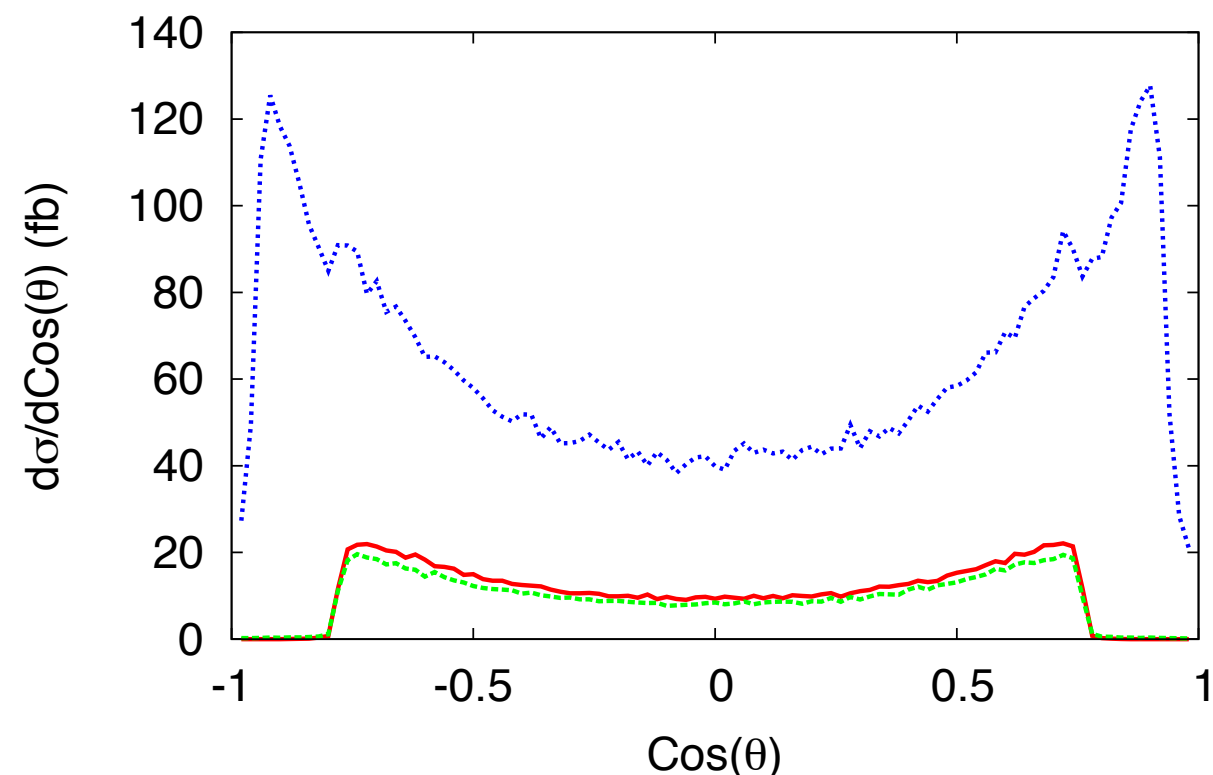
# Antlers at Lepton Colliders



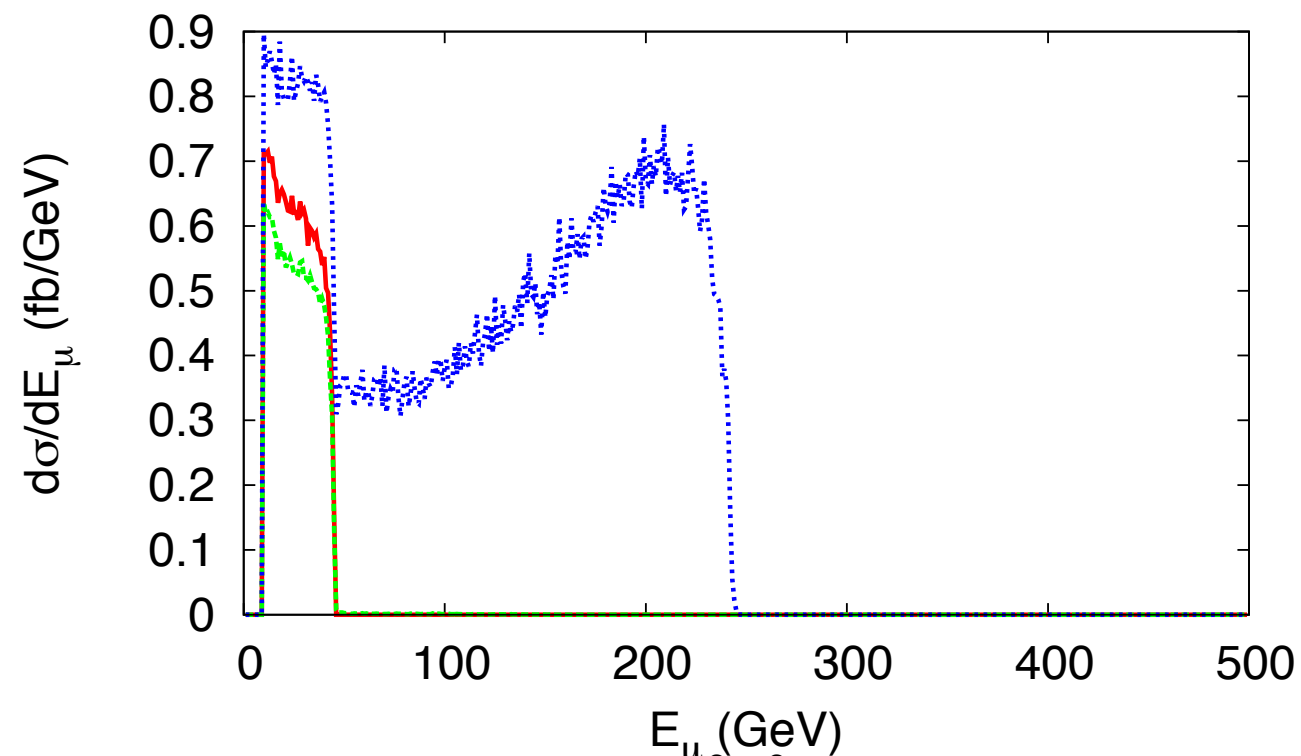
$$e^+ e^- \rightarrow \mu^+ \mu^- \tilde{\chi}_1^0 \tilde{\chi}_1^0, \sqrt{s} = 500 \text{ GeV}$$



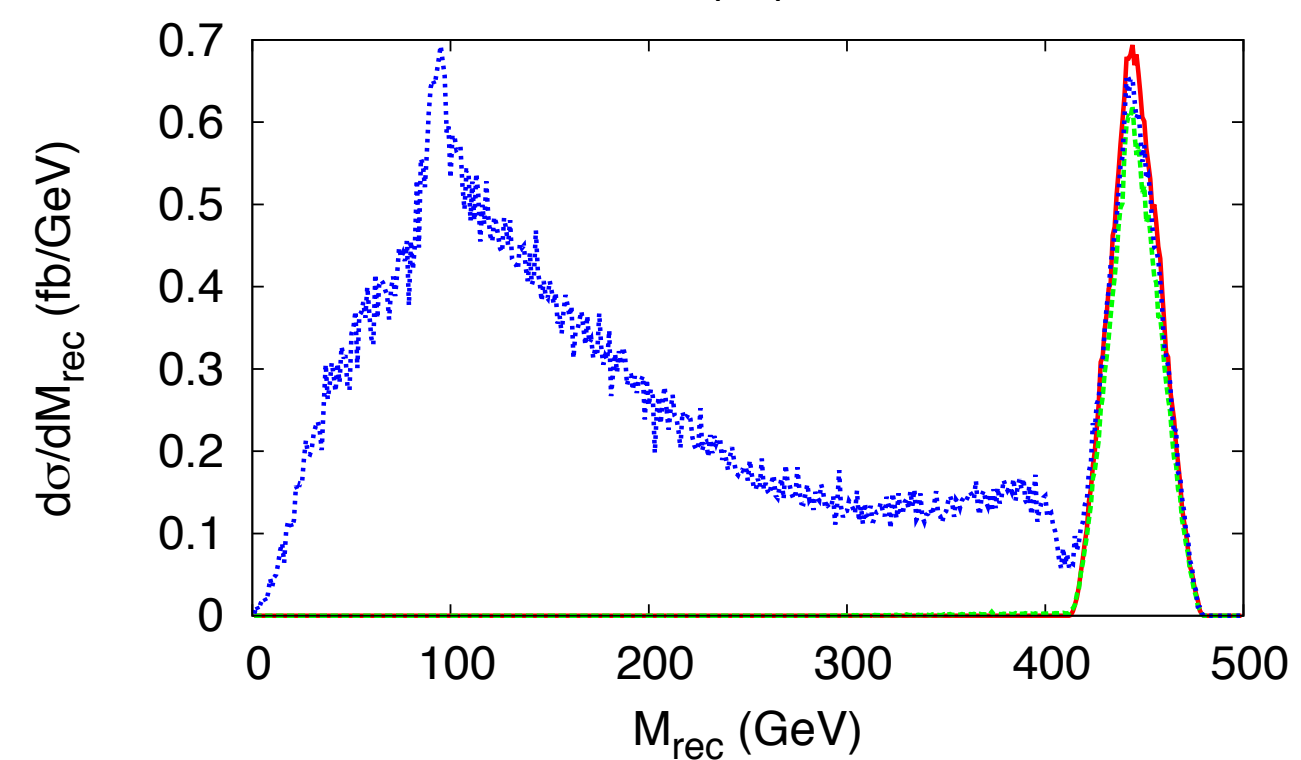
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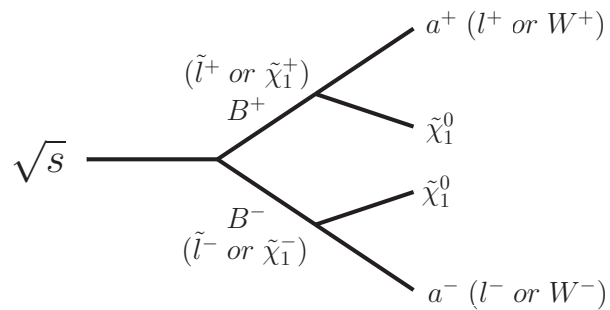


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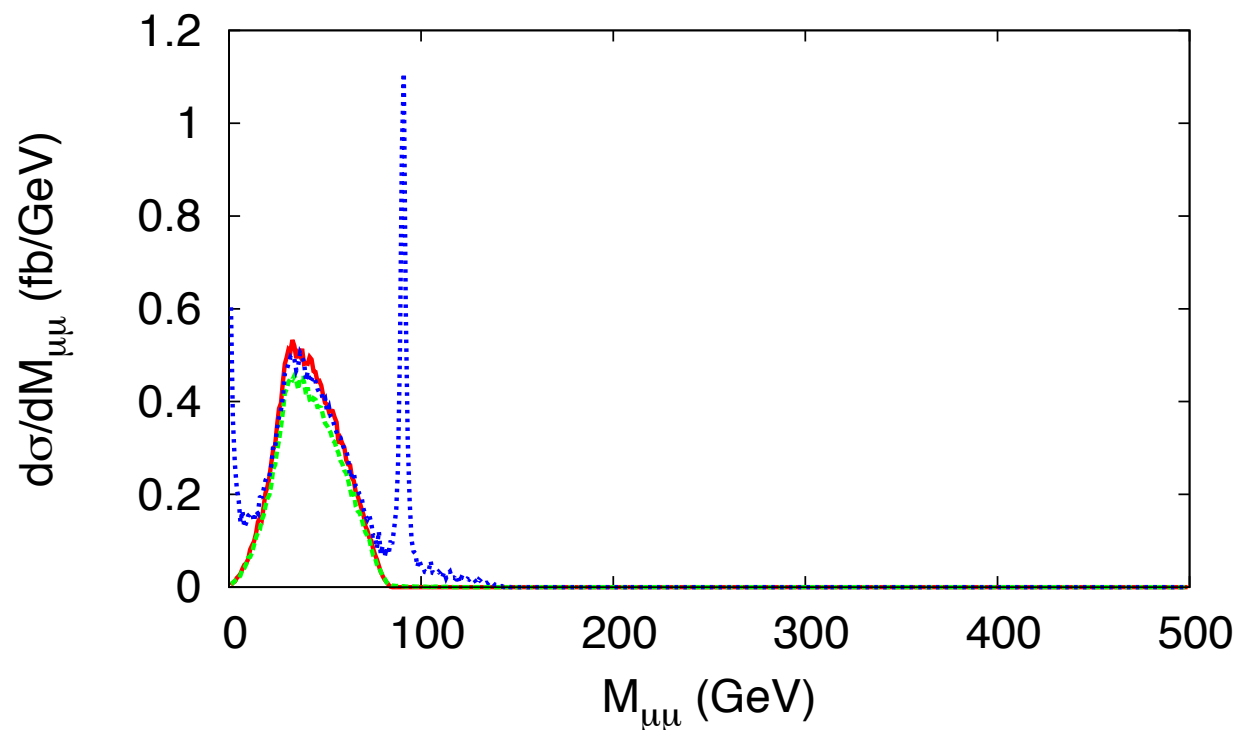
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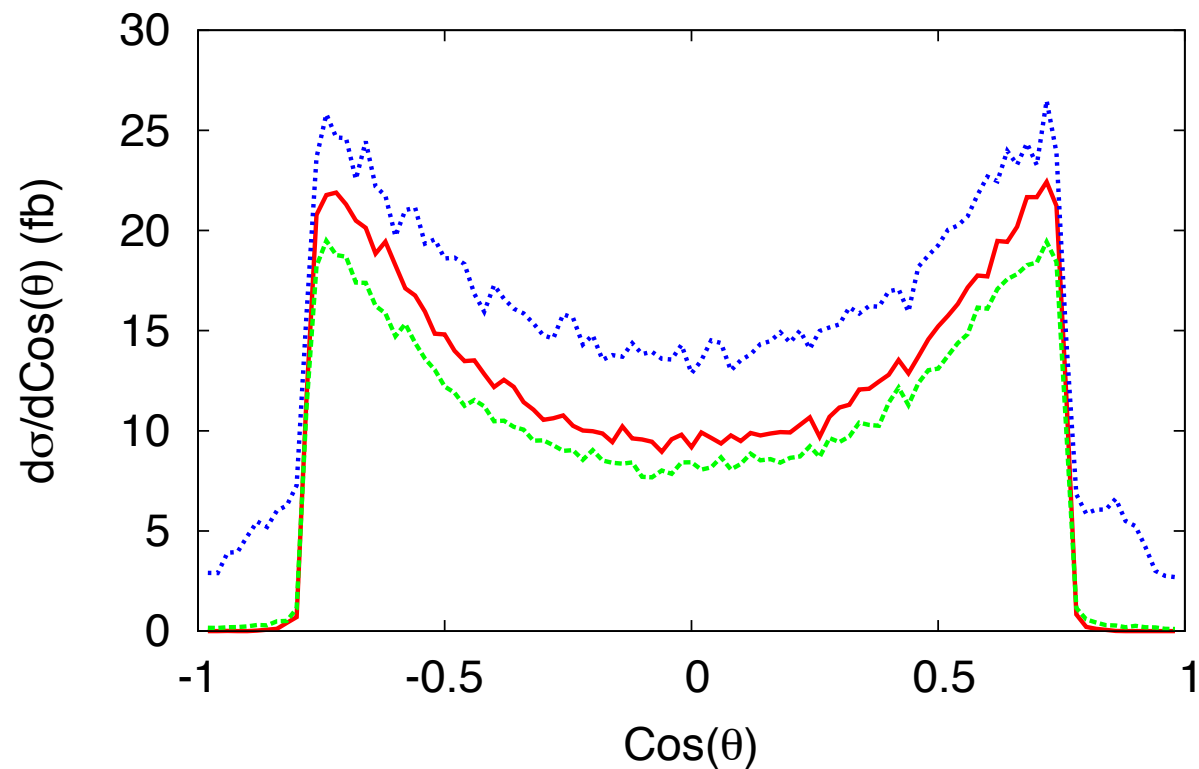


$$m_{\text{rec}} \geq 350 \text{ GeV}$$

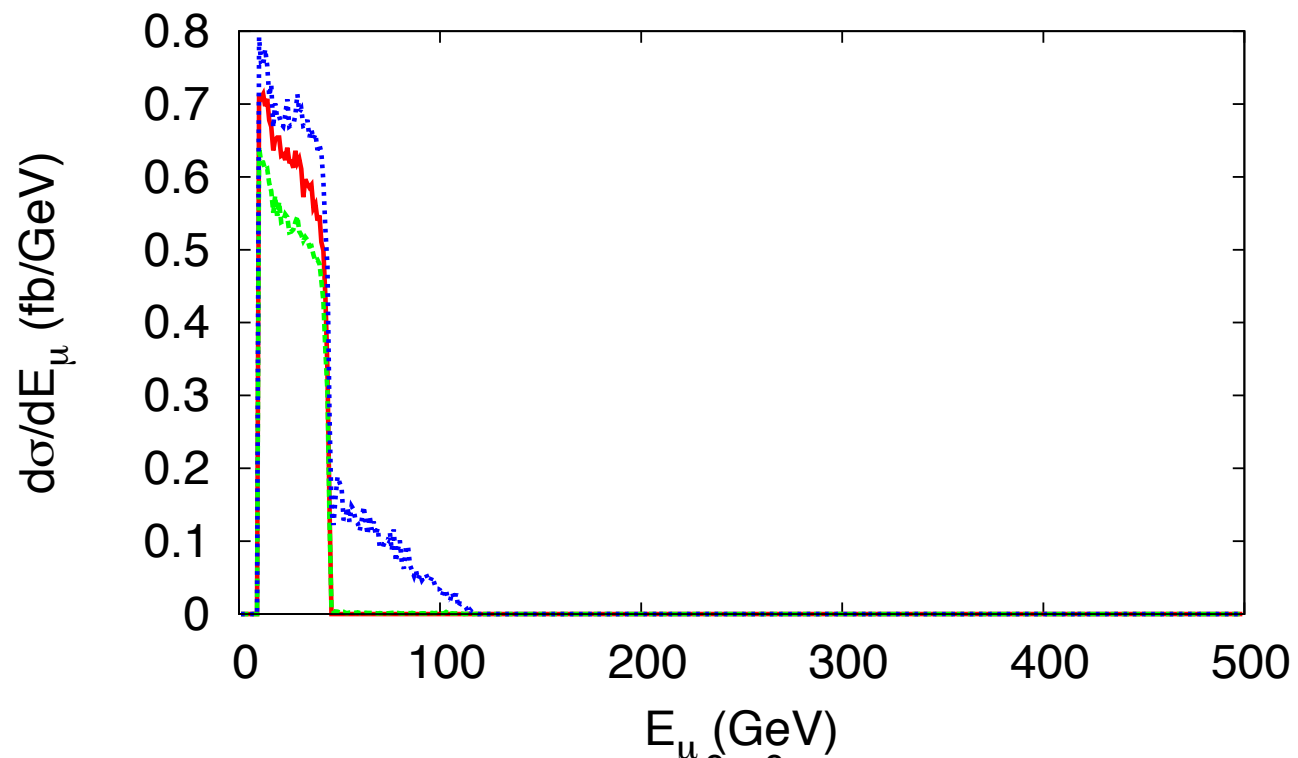
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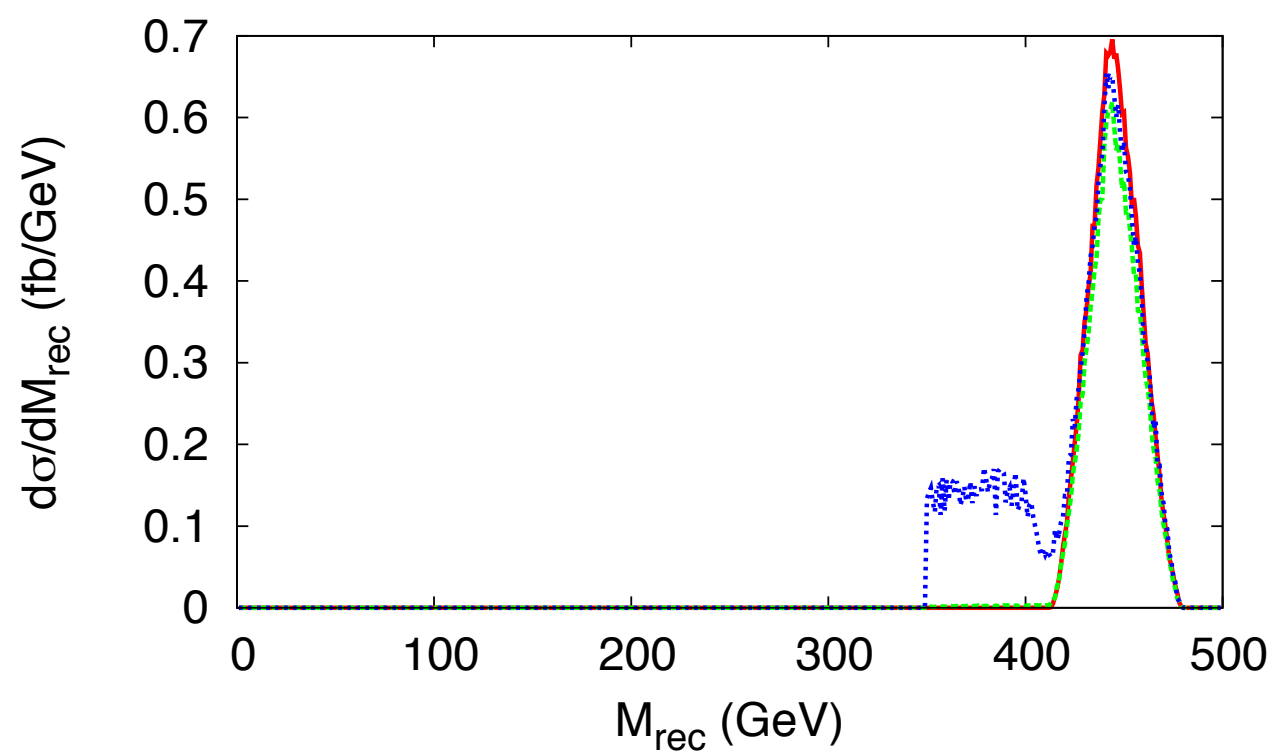
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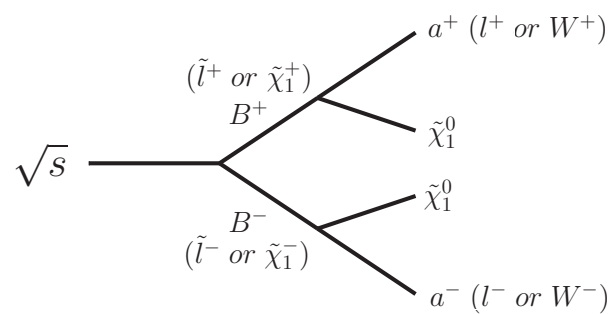


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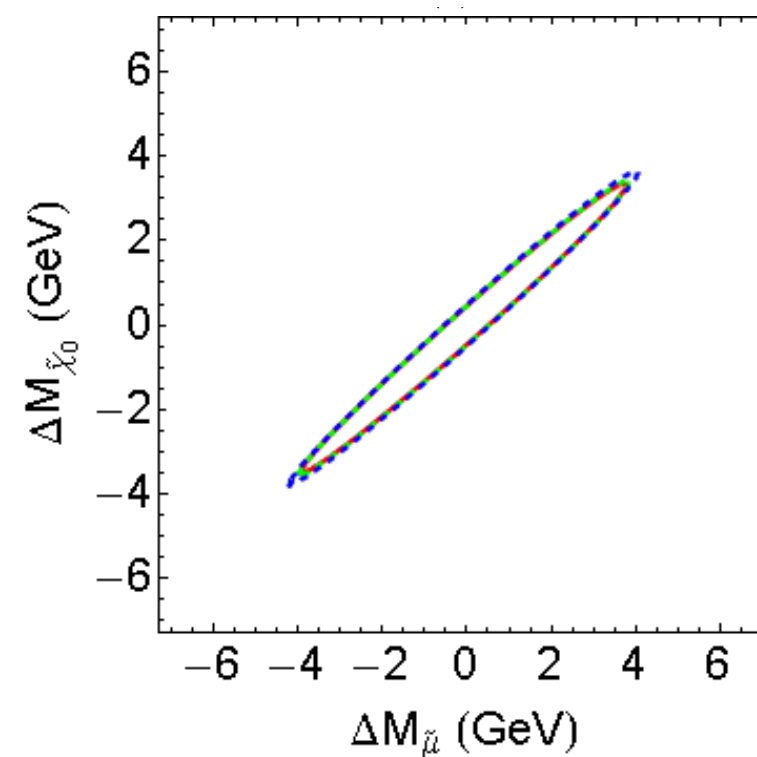
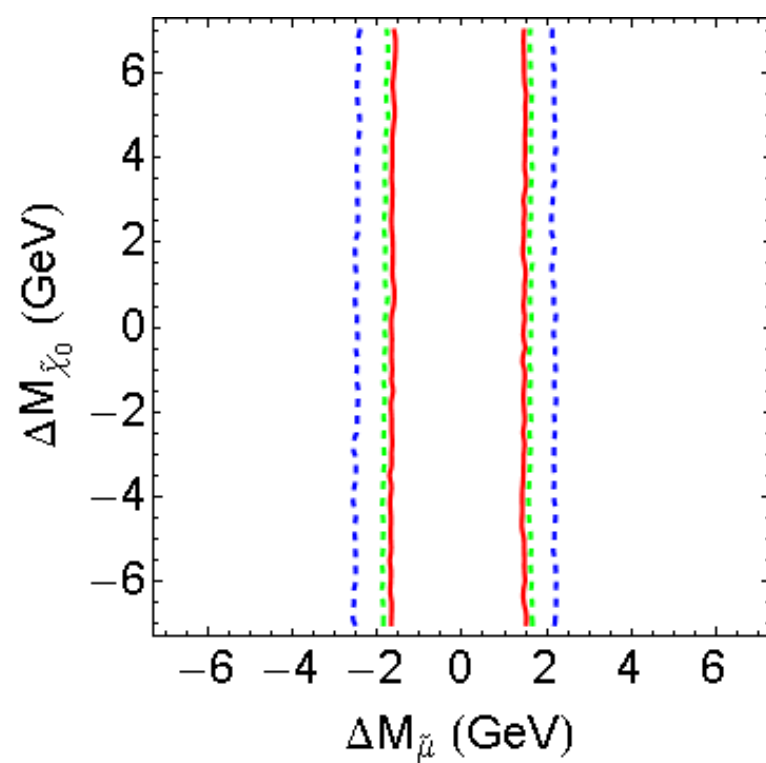
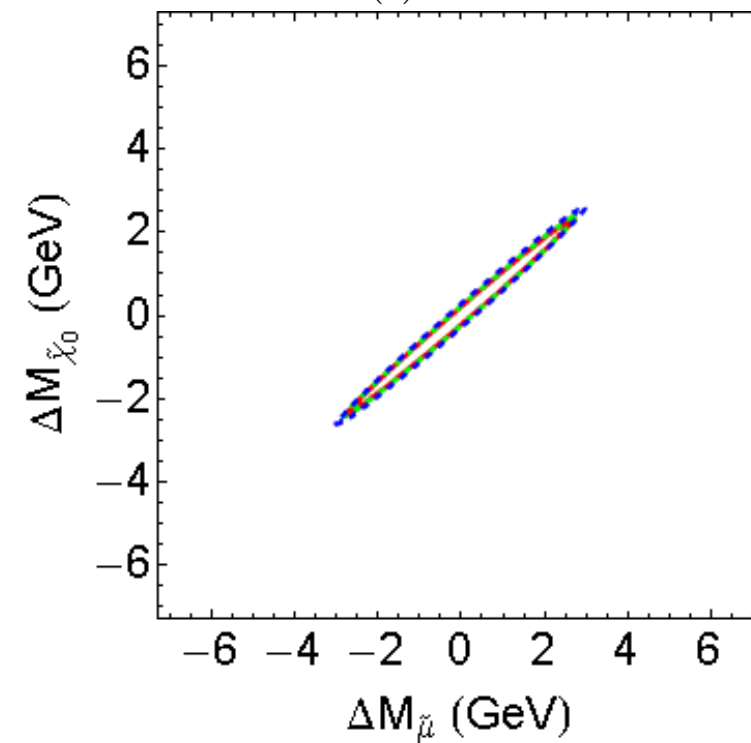
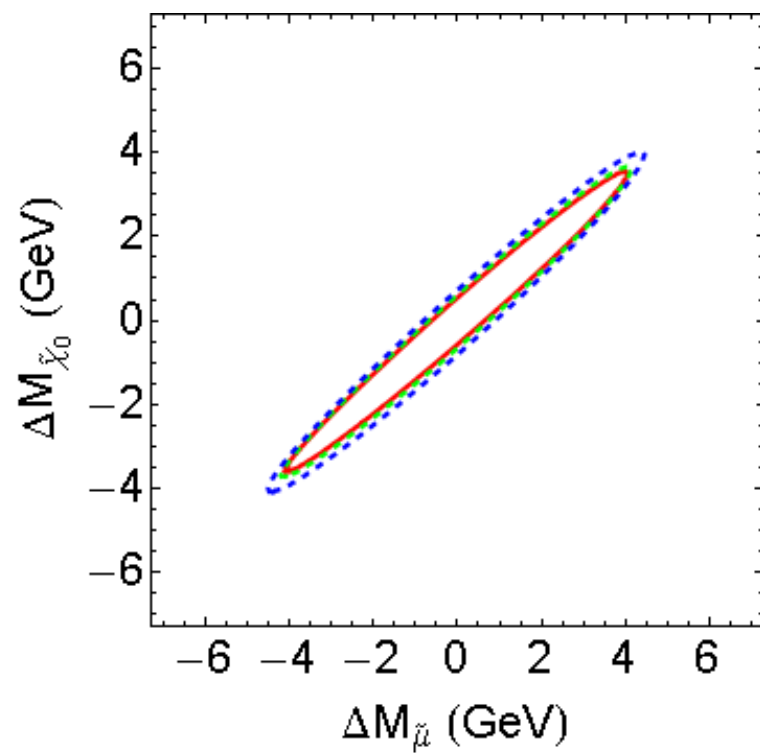


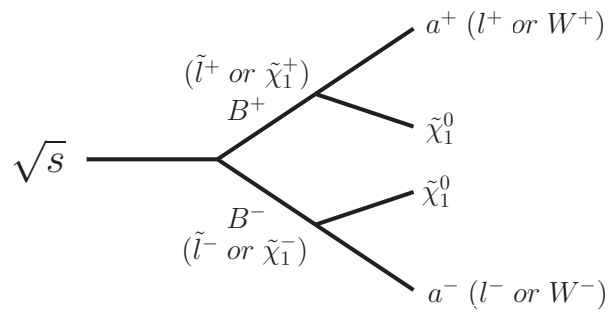
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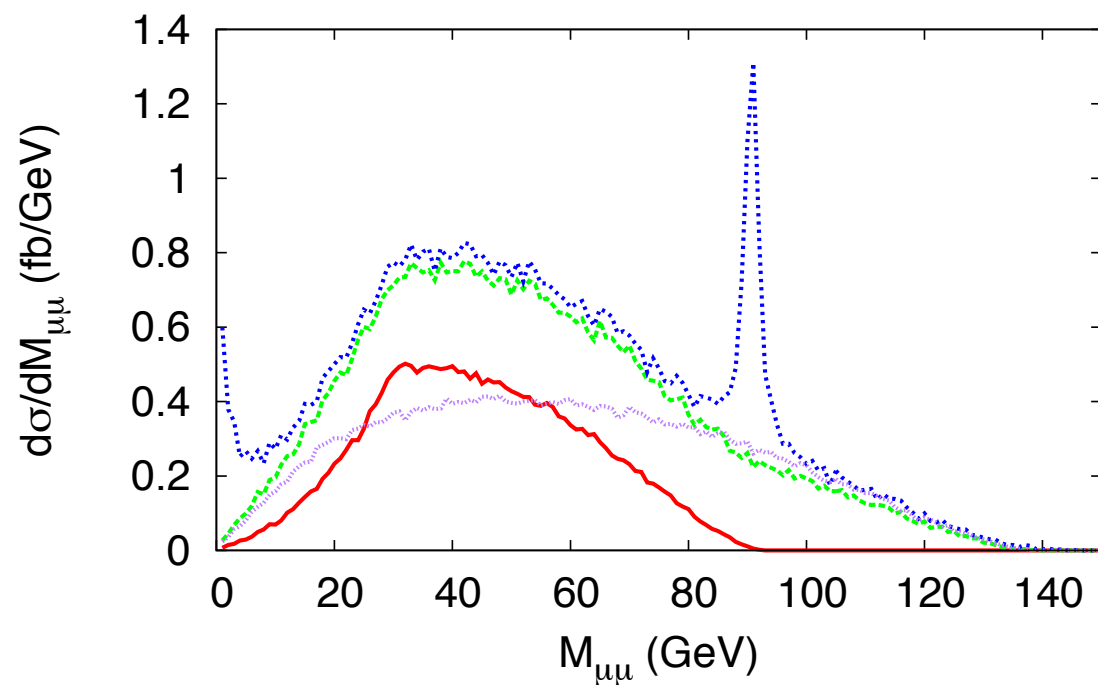


95% CL : 100fb<sup>-1</sup>

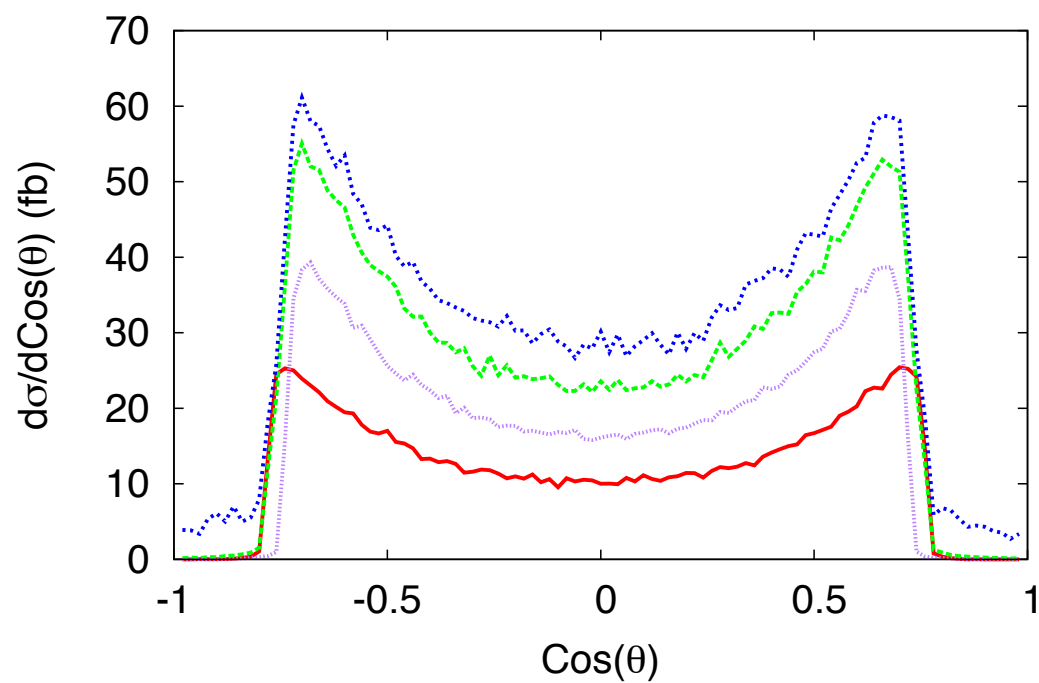




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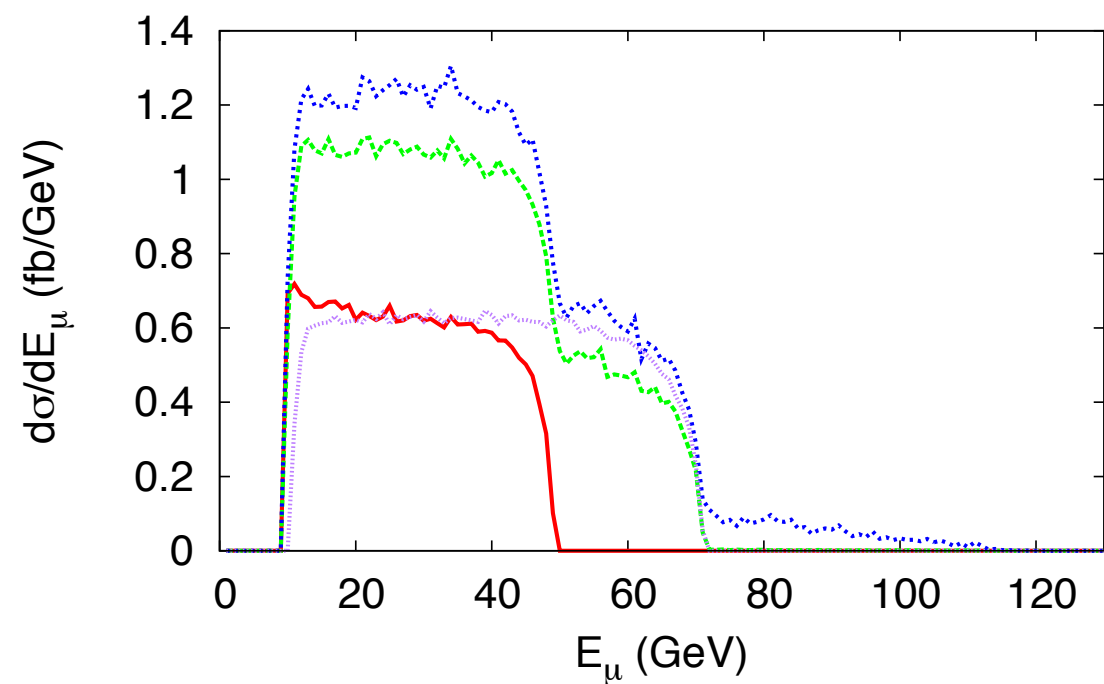


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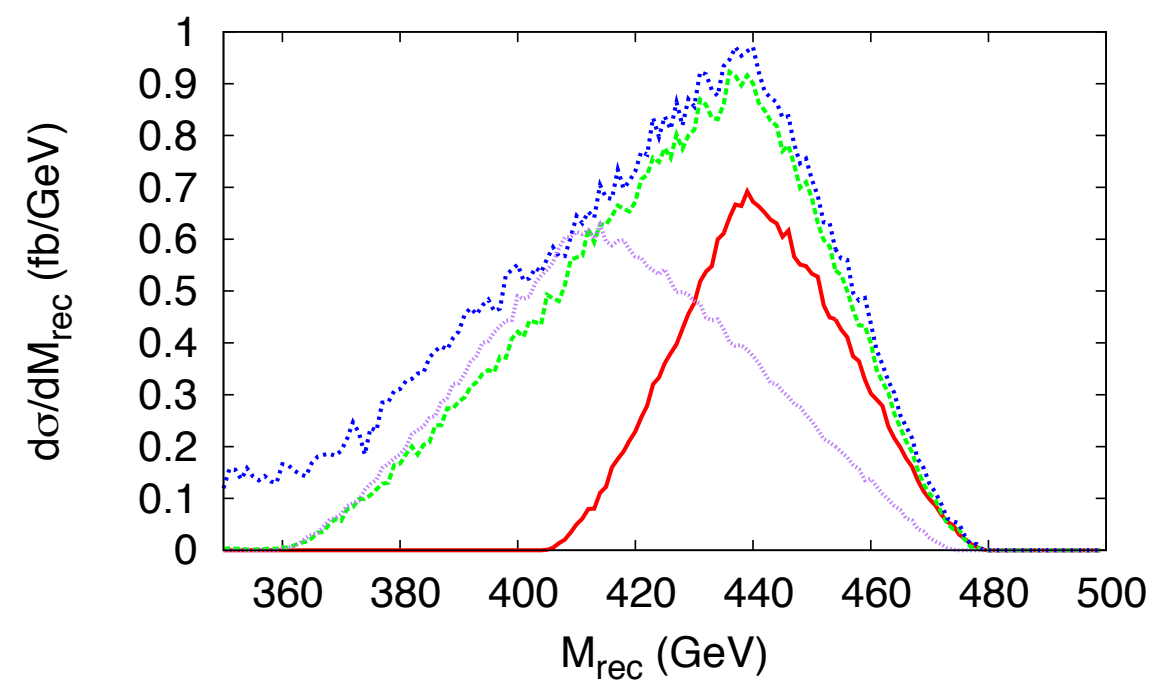


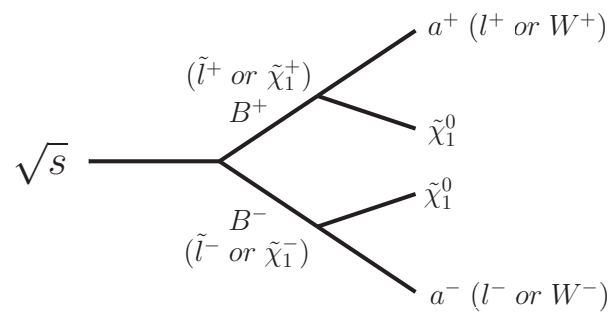
$$m_{\tilde{l}_L} \sim m_{\tilde{l}_R}$$

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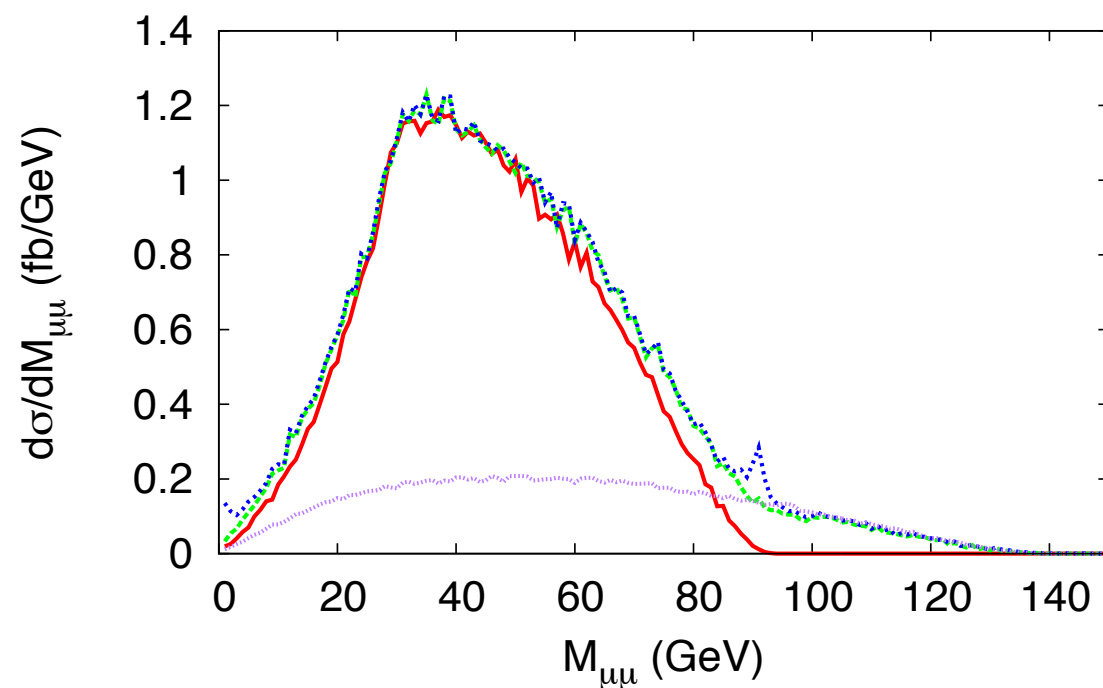




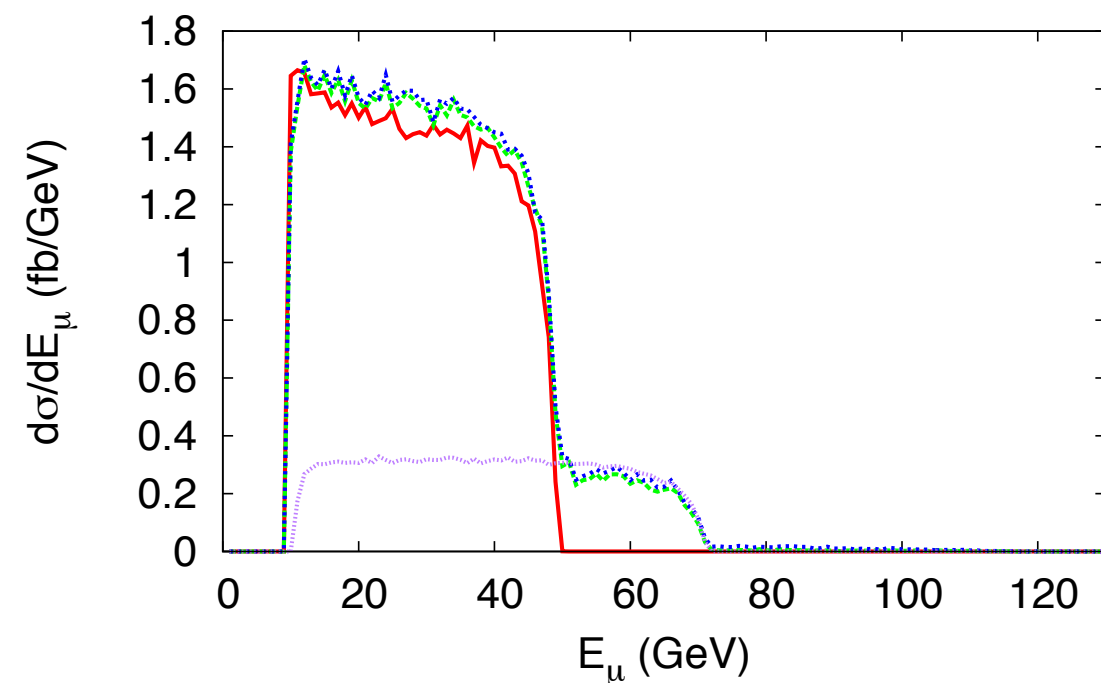
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80%:60%  
right polarization

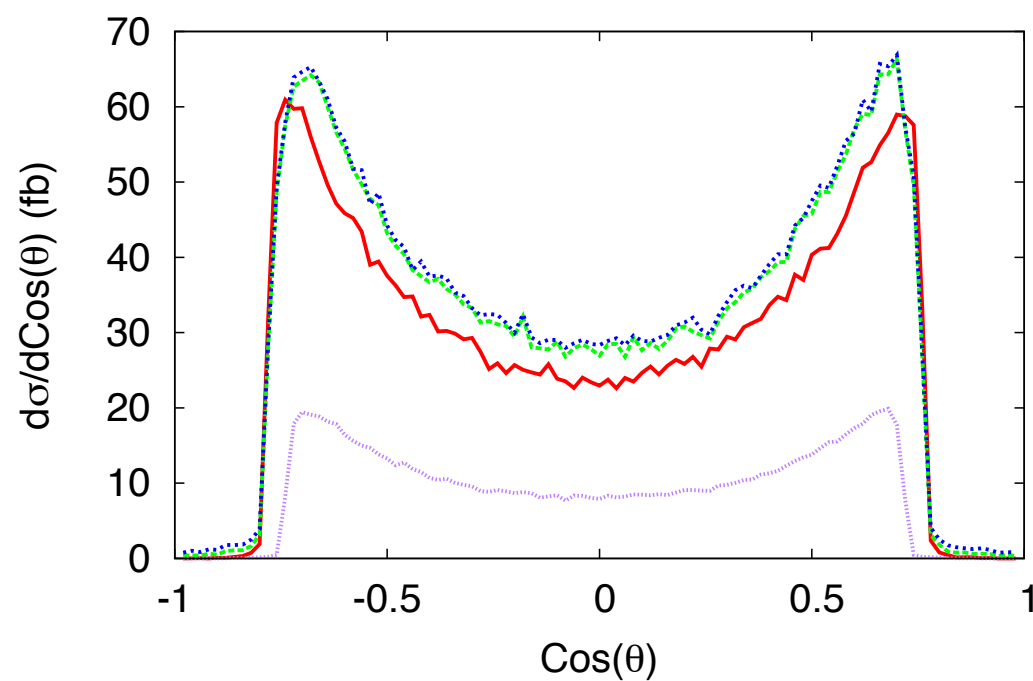
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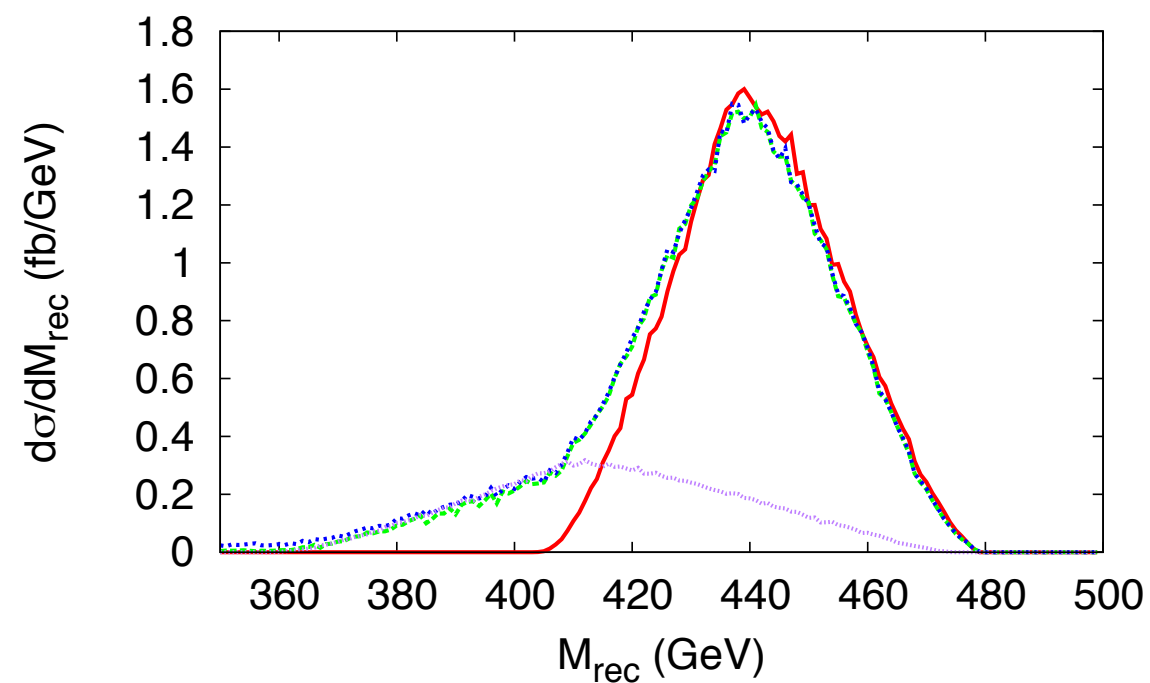
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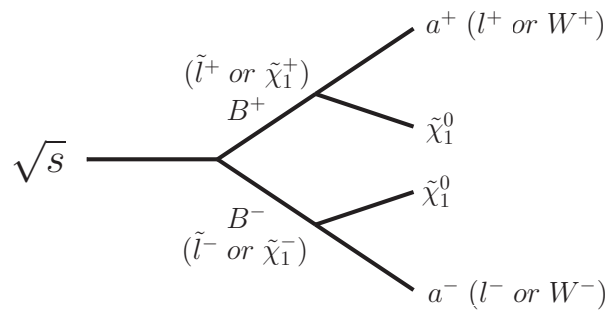
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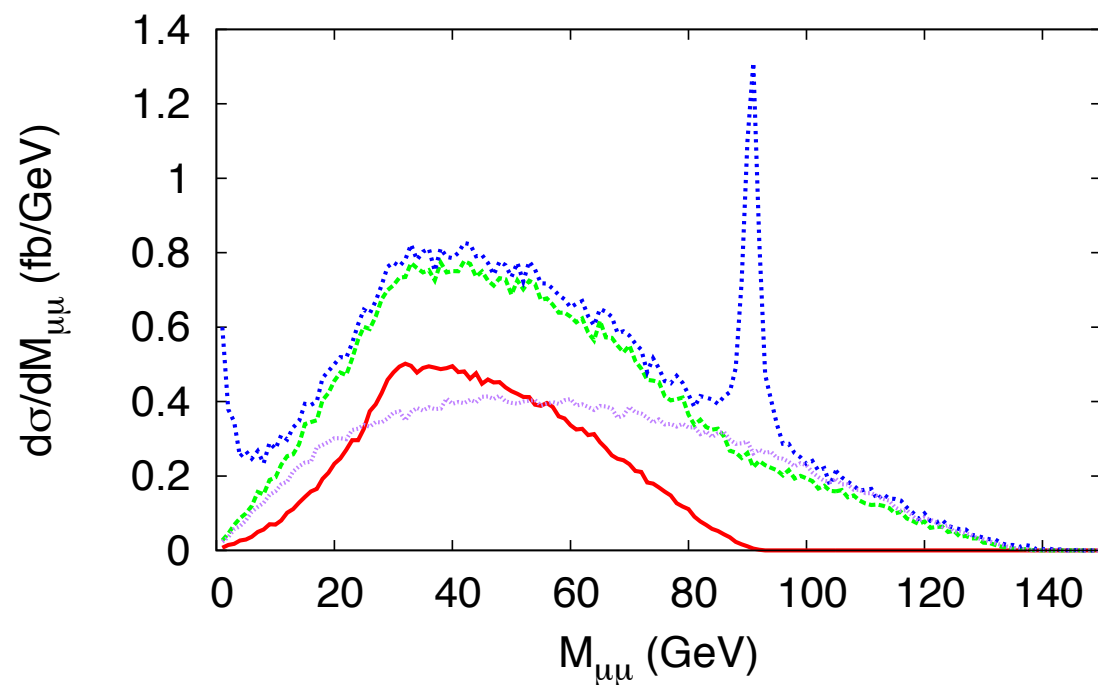
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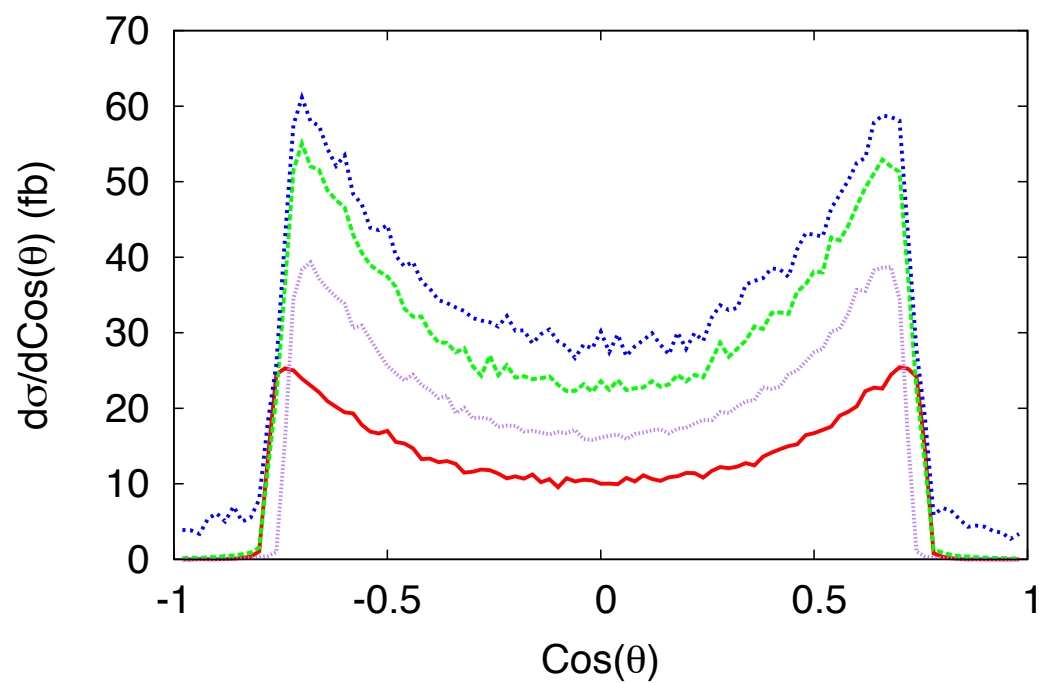




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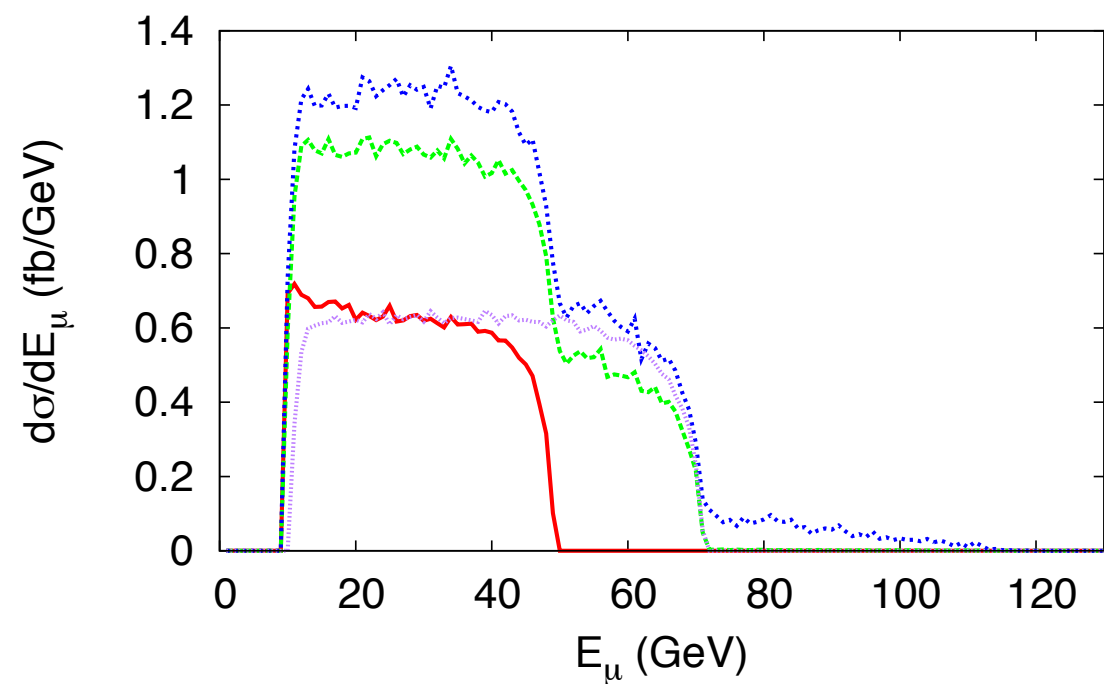


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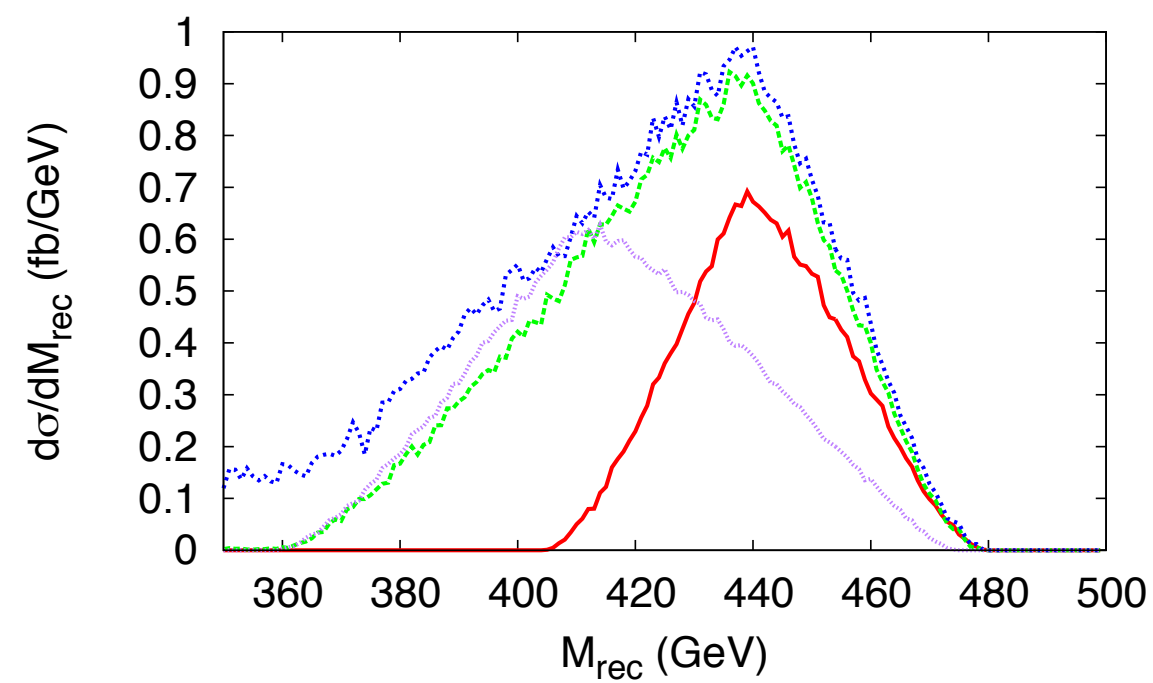


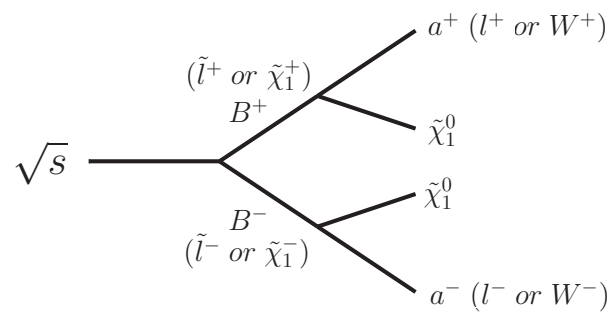
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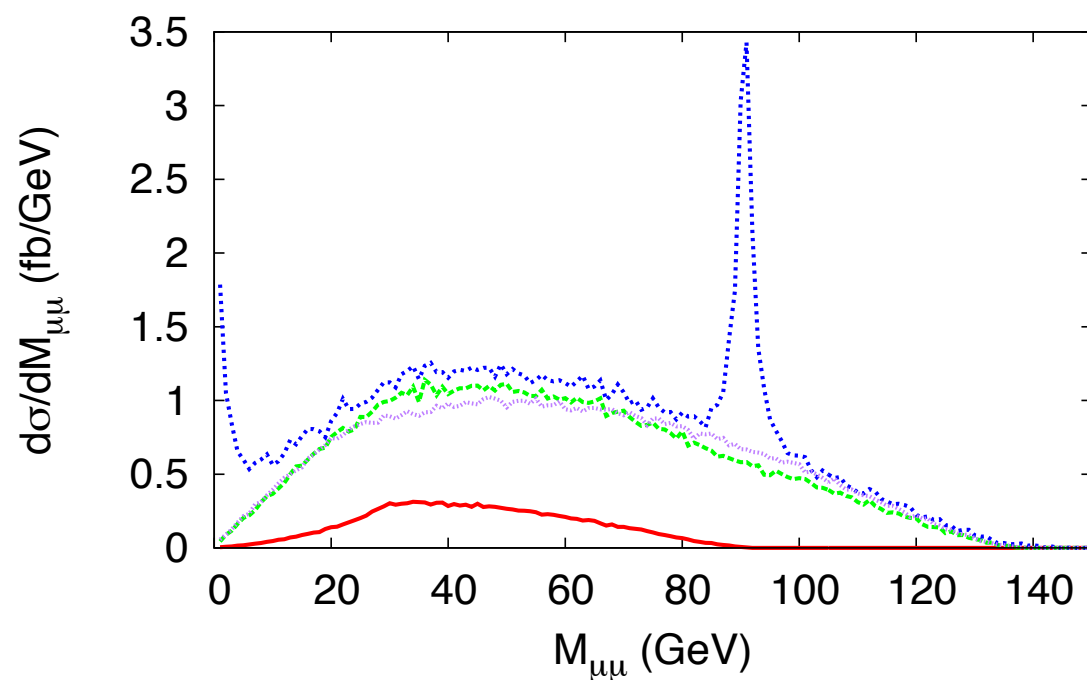




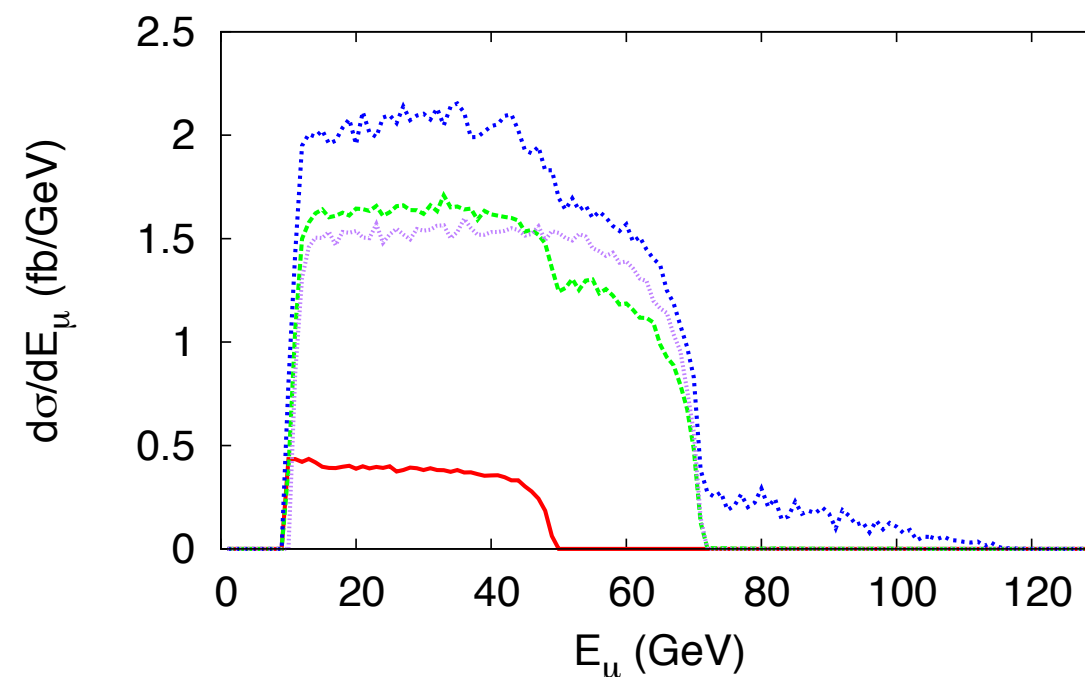
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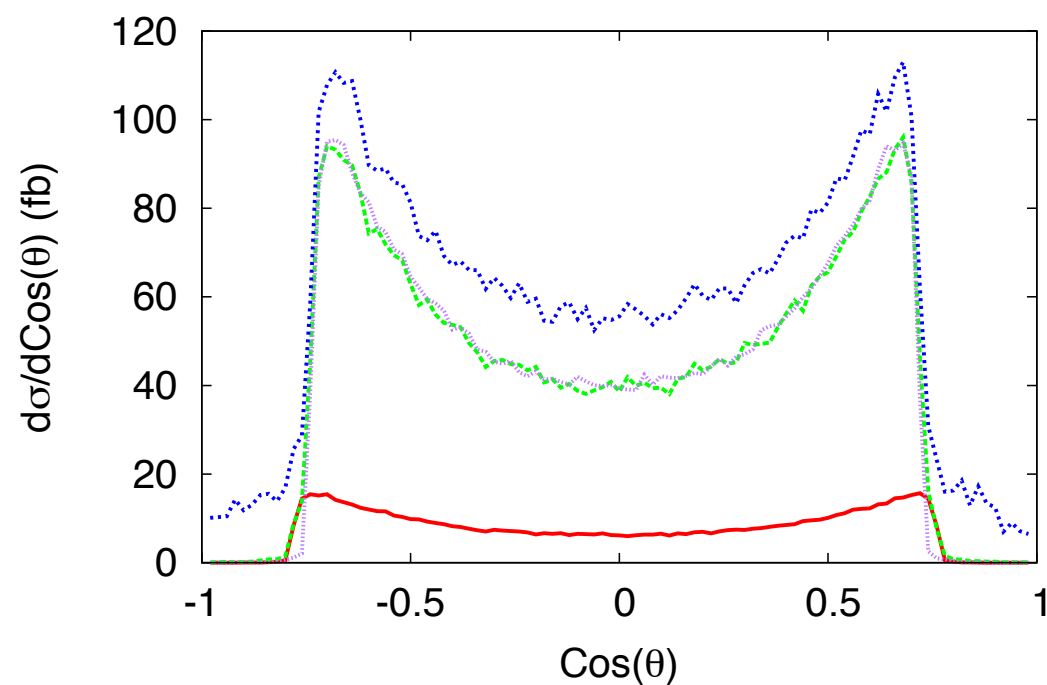
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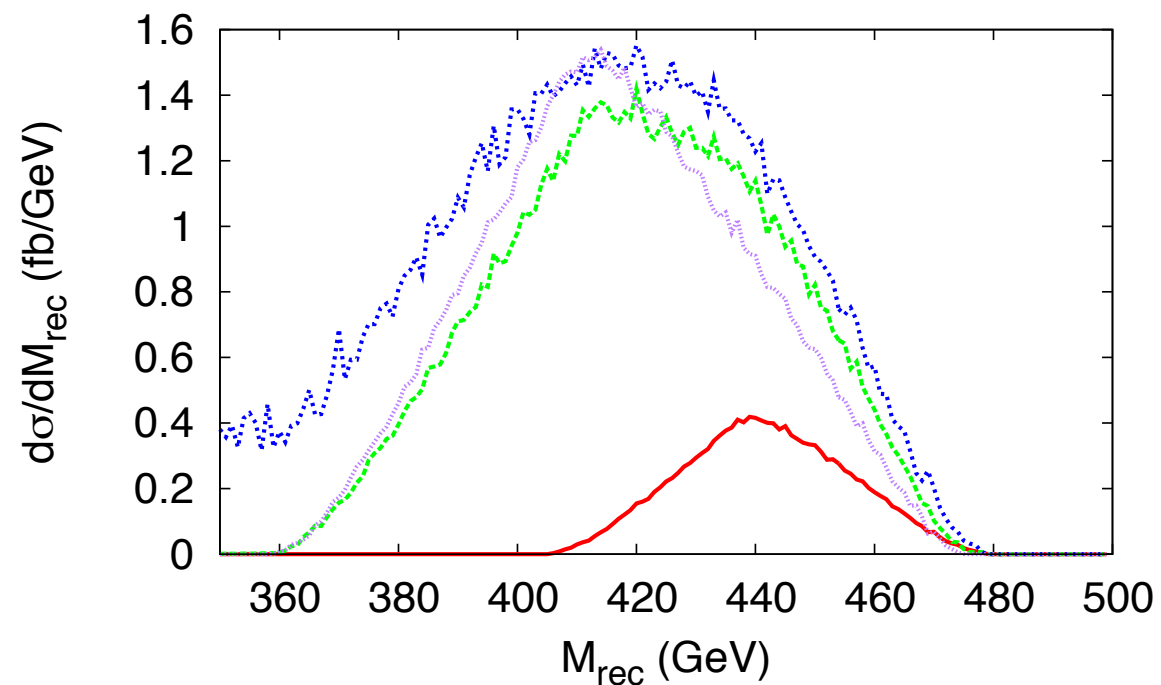
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$$e^+ e^- \rightarrow \mu^+ \mu^- \tilde{\chi}_1^0 \tilde{\chi}_1^0, \sqrt{s} = 500 \text{ GeV}$$



# Lepton Collider Mass Determination

- Lepton colliders provide a known collision frame.
  - $m_{\text{rec}}$  can be used to remove most of the SM background.
  - $\cos \theta$  endpoints not significantly smeared.
- Cusps and end points of kinematical variables of Antler diagrams give good mass measurement.
  - Improve on  $E_a$  endpoints, especially if  $E_{\text{amin}}$  is too small to be measured.
- Polarization can distinguish between  $\tilde{l}_L$  and  $\tilde{l}_R$  even if close to each other (in addition to further suppressing the SM background).

# Lepton Collider Spin Determination

$$\langle j, m', \theta | j, m \rangle = d_{m, m'}^j(\theta)$$

- What we would really like is to measure the Wigner d-functions directly.
- Dark matter particles missing: not enough information.
- If we know the masses of the particles in the Antler diagram:
  - 8 unknowns : 8 equations : However, some quadratic : 2-fold ambiguity.
- We have discovered a new way to fully reconstruct the absolute value of the angular distribution and partially reconstruct the sign.
- To be published soon: Christensen, Salmon.